

Do Cross-Sectional Stock Return Predictors Pass the Test without Data-Snooping Bias?

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Abstract

This study examines the possible data-snooping bias as a competing explanation for the anomalies in the cross-section of stock returns. We posit that the exhaustive standalone searches for profitable strategies could lead to recommending spuriously predictive variables. In order to explore the severity of this problem, we use a multiple testing method to evaluate the profitability of portfolios constructed by these predictors. Our empirical analyses suggest that over half of the findings based on individual testing method are no longer statistically significant after we adjust for data-snooping bias. Excluding the micro-cap stocks before portfolios construction and applying the notion of economic significance in this study further weaken the evidence for predictability.

JEL classification: G11, G12, G14.

Keywords: anomalies, data-snooping bias, stock return predictability, portfolio strategies.

1 Introduction

This study aims at the documented pieces of evidence for cross-sectional stock return predictability in the past decades, for which the prior studies provide two major competing explanations. The first one suggests that the earned excess returns merely serve to compensate for investors' assuming risk. For example, Hou et al. (2015) and Fama and French (2016) employ rational risk-based factor models to explain the predictability phenomena. The second explanation follows the behavioral-based theory; for example, Jacobs (2015) argues that the abnormal returns associated with the anomalies are mostly driven by investor sentiment. These explanations reinforce the attempts by financial practitioners and academic researchers to identify outperforming stock selection rules or anomalies.

In contrast, this study posits and examines the extent to which data-snooping bias could account for a substantial proportion of the significant findings of anomalies. Researchers have been searching for predictors and testing their predictive ability time and again. However, without properly adjusting the statistical inference, the studies that conduct a seemingly promising set of standalone hypothesis tests may *probably* commit Type I errors because of the repeated trials. Therefore, the collective efforts in analyzing the cross-sectional stock return predictability may mislead researchers to endorse false anomalies due to the bias in statistical inference. To mitigate the data-snooping bias problem, we collect a set of stock return predictors and conduct a simultaneous inference under one family of hypotheses such that the overall error rate is controlled.

Our study is closely related to Harvey et al. (2016), who apply a multiple testing method to estimate the adjusted critical value for t -ratios of the factor risk premium, and recommends a new threshold rule for future studies to justify a statistically significant risk factor. Our study, however, differs from theirs in two aspects. First, we focus on the mean and risk-adjusted returns of portfolios formed based on firm characteristics, while a lot of the factors studied in Harvey et al. (2016) are macroeconomic variables. Second, we employ a different multiple testing algorithm and can thus assess economic significance as well as statistical significance. That is, our method could estimate the critical values not only for the t -ratios, but also for the risk-adjusted returns.

The empirical results show that many of the predictors generating statistically significant portfolio mean returns based on individual testing methodology are no longer accurate under the simultaneous inference. The findings based on our notion of economic significance also suggest that only 15 out of the collected 135 firm characteristics effectively help construct profitable long-short portfolios. Furthermore, if we exclude micro-cap stocks before the portfolio construction, then only annual growth in split-adjusted shares outstanding could deliver

an economically significant return spread. However, its superior portfolio performance disappears if we incorporate a risk adjustment with Fama and French (2015)'s 5-Factor model or Hou et al. (2015)'s Q-Factor model. For a further perspective, we classify the predictors into multiple families of hypotheses and construct another simultaneous inference. With this research design, we are able to identify statistically and economically significant predictors from the value and momentum categories along with the net share issues for the universe without micro-cap stocks. Our subsample analyses also complement the studies by McLean and Pontiff (2016) and Jones and Pomorski (2016), whose findings imply that the profitability of anomalies is less pronounced in the out-of-sample.

The rest of this article proceeds as follows. In the next section, we briefly review how the data-snooping bias could affect the stock return predictability tests. Section 3 explains the multiple testing procedure and describes the data. We present the benchmark results based on annually rebalanced portfolios in Section 4. Section 5 discusses the results based on monthly rebalanced portfolios. Section 6 provides additional analyses to assess if our tests are unduly conservative. Section 7 presents the results over different sample periods. Section 8 concludes.

2 Data-Snooping Bias and Market Efficiency Tests

The concern for data-snooping bias in conducting market efficiency test is well-aware in the literature. For instances, Sullivan et al. (1999) and Bajgrowicz and Scaillet (2012) address the problem of data-snooping bias in testing technical trading strategies; Fama and French (2010) and Barras et al. (2010) analyze which mutual funds are outperforming simply because of data-snooping bias, or luck in their own terminology; Conrad et al. (2003) and Harvey et al. (2016) estimate the critical values for determining the significance of cross-sectional stock return premium without data-snooping bias.

To illustrate why data-snooping bias could arise, consider a hypothetical example with a large number of time-series of returns being tested against market efficiency. The returns could be of mutual funds, technical trading strategies, or portfolios of stocks. Suppose the market is efficient, i.e., all of the true expected returns are less than or equal to zero. If we test the null hypotheses of zero expected returns individually, then it will be quite likely that one of the hypotheses is rejected, even though market efficiency is not violated. To be specific, suppose the typical 5% significance level is used, then the probability of resulting in at least one false rejection, which is one minus the probability of all null hypotheses being simultaneously accepted $(1 - (1 - 0.05)^M)$, would approach one as the number of tests M gets large enough. Such inferential bias due to conducting the statistical tests individually is

usually referred as data-snooping bias (or luck in Fama and French (2010) and Barras et al. (2010)).

The above example highlights the needs to test market efficiency by a number of return series simultaneously. Conrad et al. (2003) and Fama and French (2010) use simulation approach to approximate the joint distribution of expected returns under the null hypotheses. They then compare the statistics generated from actual and simulated data to evaluate the expected returns. For example, Conrad et al. (2003) quantify how much of the value-growth premium that may be attributed to data-snooping bias by first constructing simulated portfolios through grouping the stocks with a large number of independent random noises. The mean returns of those highly ranked simulated portfolios are then used as the hurdle rate for the mean portfolio returns from actual data.

Although the simulation approach is appealing because of its intuitiveness, it is not based on a formal statistical method. In other words, the approach does not provide a certain confidence level when it identifies portfolios with superior returns above the threshold. A multiple testing framework could overcome this shortcoming by introducing a notion of error rate. Barras et al. (2010), Bajgrowicz and Scaillet (2012), and Harvey et al. (2016) control the false discovery rate (FDR), defined as the expected value of the ratio of the number of Type I errors to the total number of rejected hypotheses. Sullivan et al. (1999) apply the Reality-Check (RC) method by White (2000) that could control family-wise error rate (FWER(1)), defined as the probability of committing at least one Type I error.

In a series of studies by Hansen (2005), Romano and Wolf (2005, 2007), Hsu et al. (2010), and Hsu et al. (2014), the RC method is generalized and improved. We follow the k -Stepwise Superior Predictive Ability test (Step-SPA(k)) by Hsu et al. (2014)¹. The Step-SPA(k) controls FWER(k), the probability of committing at least k Type I errors, and has been shown to have better finite-sample statistical power in various scenarios.

There are two main differences between the procedures that follow White (2000) and the FDR controlling method in Barras et al. (2010), Bajgrowicz and Scaillet (2012), or Harvey et al. (2016). First, the former uses bootstrap to approximate the joint distribution of the test statistics and the latter needs to assume a specific form of dependence structure among the test statistics². Second, the input of FDR controlling procedure are p -values, therefore it can only obtain the critical value for the studentized test statistics (typically in the form

¹The method is introduced in the next section.

²The most celebrated FDR controlling procedure by Benjamini and Hochberg (1995) (BH) has been proven to hold under the positive regression dependence assumption. Benjamini and Yekutieli (2001) (BY) propose another procedure that could control FDR under arbitrary dependence structure. The BY's critical value is greater than the BH's since it needs to ensure FDR is bounded under the most general case. The advantage of bootstrap-based procedure, as adopted in this paper, is that it captures the dependence structure information from the data, hence it should have greater statistical power.

of t -ratios). Meanwhile, the Step-SPA(k) could provide critical value for non-studentized test statistics, i.e., the mean or risk-adjusted return itself, so it allows us to make inference on economic significance similar to Conrad et al. (2003).

3 Empirical Procedure

This section describes the empirical procedure. We first illustrate the multiple testing methodology, and then discuss the data collection and portfolio construction.

3.1 Multiple testing methodology

Simulating a typical research design in empirical asset pricing or anomaly studies, we sort the stocks into groups of portfolios based on a firm characteristic x_i at the end of every year or month. We then form a long-short portfolio based on the extreme groups and examine the resulting monthly portfolio returns with a linear factor model:

$$R_{it} = \alpha_i + \mathbf{F}_t' \beta_i + \varepsilon_{it}. \quad (1)$$

The magnitude of $\hat{\alpha}_i$ and its t -ratio are interpreted as the measures of significance of the anomaly. Here \mathbf{F}_t is one of the sets of factor portfolio returns described in Subsection 3.2.3. If \mathbf{F}_t is an empty vector, then $\hat{\alpha}_i$ is simply the estimator for mean return. We perform multiple testing on the estimated alphas from different factor models separately. A particular attention will be given to the case of mean returns to see how the data-snooping bias effect could explain the anomalies without any risk-factor models.

We tackle the problem of data-snooping bias by specifying a family of hypotheses and conducting multiple testing on it. In this study, the null hypotheses of interests are

$$H_0^i : \alpha_i \leq 0, \quad i = 1, \dots, M, \quad (2)$$

where M is the total number of portfolios to be considered in the family-wise hypothesis. If each study tests its proposed predictor x_i individually while ignoring the fact that one logically related hypothesis, i.e., whether the cross-sectional stock returns are predictable, has been tested multiple times, then there could be a potential data-snooping bias in the statistical inference.

To simultaneously test the hypotheses, we adopt the Step-SPA(k) by Hsu et al. (2014), which asymptotically controls the FWER(k) and is a generalization over Step-SPA(1) of Hsu et al. (2010). The test based on FWER(k) control could be more powerful since it allows

us to make more false rejections. In practice, such relaxation is useful, especially when the universe of hypotheses is large. However, we also do not tolerate too many Type I errors. To choose k below 3 is typically suggested; for example, see the simulation results in Romano and Wolf (2007) and Hsu et al. (2014).

The step-by-step implementations of Step-SPA(k) procedure are explained in Appendix A. There are two versions of test statistics, studentized and non-studentized, that could serve different purposes. To explain the procedure intuitively, we use the non-studentized test statistics as an example here. Let \mathcal{H}_0 denote the set of index where the portfolios have true $\alpha_i \leq 0$. The goal of multiple testing method is to derive a critical value to separate the significant strategies from the ones in \mathcal{H}_0 while also controls FWER(k) below the level δ . The definition of FWER(k) suggests a valid critical value $CV(k, \delta)$ should satisfy the following:

$$\begin{aligned} \text{FWER}(k) &= \mathbb{P} \{ \text{Reject at least } k \text{ of hypotheses in } \mathcal{H}_0 \} \\ &= \mathbb{P} \left\{ \text{The } k\text{-th largest value of } \{ \sqrt{T}(\hat{\alpha}_i - \alpha_i), i \in \mathcal{H}_0 \} > CV(k, \delta) \right\} \\ &\leq \delta. \end{aligned}$$

In practice, we do not know \mathcal{H}_0 . Therefore, the stepwise procedure starts with $\mathcal{H}_0 = \{1, \dots, M\}$ to obtain the most conservative critical value and then refines the choice of \mathcal{H}_0 in the next steps until no further improvement. As for the probability distribution of joint high-dimensional order statistics, Step-SPA(k) adopts the bootstrap method as an approximation; see Step (S4)–(S9) in Appendix A for further details. Therefore, the dependence structure among the test statistics is implicitly taken into consideration from the data. The final output of the Step-SPA(k) algorithm is $CV(k, \delta)$ that serves as a cut-off point to distinguish between the significant and insignificant strategies.

The adjusted critical value for t -ratios is obtained by applying Step-SPA(k) algorithm on the studentized test statistics. That is, we use $\sqrt{T}(\hat{\alpha}_i - \alpha_i)/\hat{\sigma}_i$ as the test statistics, where $\hat{\sigma}_i$ is the consistent estimator for the standard deviation of $\sqrt{T}(\hat{\alpha}_i - \alpha_i)$. Due to the multiplicity of testing related hypotheses, the adjusted critical value would be greater than 1.96, the quantile of two-sided test with 5% significance level based on univariate Gaussian distribution. Taking the non-studentized test statistics as the input of Step-SPA(k) algorithm would produce the critical value for alphas. We interpret this hurdle rate as the magnitude of the mean or risk-adjusted portfolio returns that should attain to be economically significant in supporting predictability after one adjusts for data-snooping bias. It makes use of the fact that the k -th best portfolio in \mathcal{H}_0 could generate $\sqrt{T}\hat{\alpha}$ as high as $CV(k, \delta)$ with $100(1 - \delta)\%$ confidence level, so that a truly superior predictor should earn an $\sqrt{T}\hat{\alpha}$ greater than $CV(k, \delta)$.

We also note that the multiple testing differs from a joint test of $H_0 : \alpha_i \leq 0, i =$

$1, \dots, M$, in which the GRS or GMM test, is usually utilized. A joint test examines an individual hypothesis of multiple parameters. Therefore, a rejection of the joint test leads to the conclusion that at least one of the alphas is significant but the researcher is clueless as to which or how many of them are significant, while the objective of a multiple testing is to distinguish between significant and insignificant alphas.

3.2 Data and portfolio construction

We retrieve the monthly stock returns from CRSP and follow the procedure outlined in Beaver et al. (2007) to adjust the stock returns for delisting bias. Unless stated otherwise, the monthly portfolio returns sample begins from July 1968 and ends in December 2015 that constitutes 570 observations.

3.2.1 Predictors

We collect a total of 135 annual predictors. There are 101 predictors calculated using Compustat Annual, among which 48 financial ratios come from Ou and Penman (1989), and the rest of them are firm characteristics that have been studied in the asset pricing or anomalies literature, either published or working papers. The remaining 34 predictors are constructed by using the data from stock prices and trading volume in CRSP. We present the definitions and references of these predictors in Table B1. Whenever the Compustat Annual data serve to form portfolios, we include only the firms with December fiscal year end to avoid look-ahead bias and exclude the financial firms (two-digit SIC code 60–67). The stocks with negative book value of equity are also excluded. Some of the predictors here overlap with the 80 anomalies studied in Hou et al. (2015) and the 100 firm characteristics in Green et al. (2014). The 135 variables in this study should provide a broad enough coverage of the predictors.

3.2.2 The universe of portfolios

Our baseline empirical analyses use annually rebalanced portfolio strategies. We follow the convention in literature to group the stocks into decile portfolios at the end of June every year. We then form the value-weighted long-short portfolios of the extreme groups and rebalance annually. To construct the universe of long-short portfolio returns, we consider two strategies for each of the firm characteristics: the first one is to long the highest-ranked portfolio and to short the lowest-ranked portfolio; the second one is to long the lowest-ranked portfolio and to short the highest-ranked portfolio. Therefore, if we have N firm characteristics, the family of hypotheses comprises $M = 2 \times N$ alphas. By considering two directions of long-short portfolio

strategies for one predictor, we assume no a priori knowledge regarding the sign of relation between this predictor and the stock returns. We use superscripts lh and hl to indicate that the long-short portfolios are low-minus-high and high-minus-low, respectively.

3.2.3 Factor portfolio returns

To calculate the risk-adjusted returns, we consider five linear factor asset pricing models. The first four models are: CAPM or single index model, Fama and French (1993) 3-Factor model, Carhart (1997) 4-Factor model, and Fama and French (2015) 5-Factor model. The data for these factors are downloaded from Professor Kenneth French’s website. The fifth model is Hou et al. (2015) Q-factor model. We follow the factor construction method in Section 2.1 of Hou et al. (2015). Since the measurement of profitability factor requires the information of earnings announcement date (Compustat Quarterly item RDQ), which are available after 1972, the estimation of alpha based on Q-factor model would use only the portfolio returns from July 1972 to December 2015.

4 Empirical Results

This section presents the baseline results of our empirical investigation on cross-sectional stock return predictability. The first subsection discusses how the data-snooping bias alone could affect the conclusion on identifying anomalies in the cross-section of stock returns. We then simultaneously test if the predictors could generate significant risk-adjusted returns in the next subsection. In the final subsection, we provide summary for some of the selected anomalies.

4.1 Analysis without risk factor model

Tables 1 and 2 present the number of rejections for the universes of annually rebalanced portfolios based on the studentized and non-studentized statistics, respectively. Their corresponding critical values $CV(k, \delta)$ are shown in parentheses. We choose to control the FWER(k) below $\delta = 5\%$ for $k = 1, 2$, and 3 . For the studentized test statistics, Newey-West standard error with lag parameter equaling 4 is used to estimate the standard deviation parameter. For comparisons, we also present the number of rejected hypotheses based on individual testing method in the column “ $t > 1.96$ ” of Table 1. In the non-studentized tests, there is no corresponding cut-off point, thus we do not report the number of rejections based on individual testing.

Panels A–D of Tables 1 and 2 report the results using different universes of portfolios. Since it is prevalent for academic researchers to use decile portfolios, the results in Panel A would serve as our base case. We also present the results in Panel B, where the stocks are grouped into quintiles. Next, we follow Lewellen (2015) to consider two universes of portfolios labeled as “all-but-tiny” and “large-cap” stocks, and report their corresponding results in Panels C and D, respectively. The all-but-tiny stocks universe is a subsample where micro-cap stocks, defined as firms with market capitalization smaller than the NYSE 20% quantile at the end of June each year, are excluded. Lewellen (2015) and Fama and French (2016) suggest that the all-but-tiny universe can be used to check if the profitability of a portfolio is mostly driven by micro-cap stocks. In the large-cap universe, we constrain our sample to the stocks with market capitalization greater than the NYSE median at the portfolio formation time. This large-cap stocks subsample helps us examine whether the anomalies still exist in the population of stocks where market efficiency is more likely to hold.

By examining the difference between the numbers of rejections under multiple testing and individual tests in Table 1, we could assess how severe the data-snooping bias is. Without using any factor models, our long-short decile portfolios sample contains 41 (out of 135) significant anomalies if we test them individually. Nevertheless, only 9 out of the 41 are still significant according to the test that controls FWER(1). If we choose less stringent error rate, FWER(3), there are still more than 50% of the rejections which may be spurious findings. When we construct the portfolios using quintile breakpoints, the overall mean return dispersions become less significant. Based on $CV(3, 5\%)$, the number of rejections is 13 compared to 16 in the decile long-short portfolios.

Panel C of Table 1 shows the number of rejections where the micro-cap stocks are excluded before the decile long-short portfolios construction. While the significant anomalies do not disappear entirely, the numbers of rejections decrease substantially. It suggests that many of the profitable long-short portfolios are not exploitable by most investors since they depend on the micro-cap stocks. For the large-cap stocks universe, the numbers of rejections further decrease. In Panel D of Table 1, only 4 of the portfolios are with mean return dispersion remaining to be significant based on $CV(3, 5\%)$. If the data-snooping bias remains being unadjusted for, there are still 24 statistically significant anomalies even when we focus on the relatively more efficient stock market universe.

For the non-studentized test, the overall numbers of rejections are much smaller than the ones based on the studentized test. The non-studentized $CV(3, 5\%)$ is 0.78% without any risk adjustment in all stocks universe. This implies that the mean return spread has to be at least 0.78% to be claimed economically significant while also maintaining the probability of getting at least 3 false rejections under 5%. Based on the most conservative error rate FWER(1),

the number of portfolios with significant mean returns is only 5. For the “all-but-tiny” stocks universe, there is only 1 long-short portfolio that can produce economically significant return dispersion based on $CV(2, 5\%)$.

Table 2 also shows that the hurdle rates for the universes of all-but-tiny and large-cap stocks are less than the ones for all stocks universe. For example, $CV(2, 5\%)$ for all stocks universe is 0.845, while the corresponding value for all-but-tiny stocks is 0.805. The exclusion of micro-cap stocks appears to reduce portfolio returns. Accordingly, the distribution of k -th largest portfolio mean return in \mathcal{H}_0 would also shift to the left. In spite of the decrease in threshold for economic significance, the number of rejections does not increase. Our results seem to echo Goyal and Welch (2008), who suggest that the economic significance of a time-series equity premium prediction model is harder to attain than the statistical significance.

4.2 Analysis with risk factor model

The multiple testing results for risk-adjusted returns suggest that some of the asset pricing models may be misspecified and thus fail to fully explain the cross-sectional stock return premium. Specifically, if a linear factor asset pricing model captures the return dispersions generated by the predictors, we should observe fewer rejections. However, this is not the case for all of the factor models. There are even more statistically significant alphas in the cases where we use CAPM, 3-Factor, and 5-Factor models.

In contrast, the 4-Factor and Q-Factor perform better. For the Q-factor model in Panel A of Table 1, there are 19 significant alphas after the risk adjustment under individual testing. If we control for FWER(3), there remain only 3 rejected anomalies. If we choose the most stringent error rate, FWER(1), then we would find no rejections at all. The pricing performance of 4-Factor model could be as well as that of Q-Factor model if we remove the tiny stocks. Panel C of Table 1 shows that there are only 2 rejections by the 4-Factor and Q-Factor models based on $CV(3, 5\%)$.

The critical values $CV(k, 5\%)$ may slightly vary with the choice of factor models, grouping methods, and universes of stocks. $CV(1, 5\%)$ ranges approximately between 3.35 and 3.54. When we relax the possible number of false rejections to 3, the critical value becomes as low as 2.75. The rule of thumb by Harvey et al. (2016), who state that the new critical value for t -ratio is 3.0, may correspond to $CV(2, 5\%)$ or $CV(3, 5\%)$. For instances, Panel A of Table 1 shows that the rule $t > 3.0$ effectively controls FWER(3), but not FWER(2), for Q-Factor alpha. Meanwhile, in the case of mean returns, $t > 3.0$ serves to control FWER(2).

For the evaluation based on economic significance in Table 2, the results in Panel C show that there are no more than 2 rejections by the 4-Factor and Q-Factor models. The significant

predictors identified by different risk factor models appear to vary. For example, the only significant portfolios that are not explained by the 4-Factor model in the “all-but-tiny” stocks universe are net share issues, **issue^{lh}** and **issue5^{lh}**. However, the net share issues premium are explained by the Q-Factor model, and the alpha that is not captured by the Q-Factor model turns out to be the result from firm characteristic **invest_LWZ^{hl}**.

4.3 Discussion of selected anomalies

This subsection discusses the results for some of the popular anomalies in detail. In each category, we report the $\hat{\alpha}$'s and t -ratios for the long-short decile portfolios based on several representative firm characteristics.

Value-growth premium. Panel A of Table 3 shows the mean returns and alphas for value-minus-growth portfolios across various factor models. The strategies **bm^{hl}** and **sp^{hl}** have the greatest return premium among the value-minus-growth portfolios in all stocks universe. After we remove the micro-cap stocks, the spreads for **bm^{hl}** and **sp^{hl}** decrease from 0.9% and 1.04% to 0.57% and 0.71%, respectively. Furthermore, while the t -ratios still exceed 2, they are no longer significant if we control FWER(3). The strategy **cfp^{hl}** is more profitable in the all-but-tiny stocks than the all stocks universe. It has 0.7% mean return spread, slightly below the non-studentized $CV(3, 5\%)$, and t -ratio above the corresponding $CV(3, 5\%)$.

The 3-Factor, 4-Factor, and 5-Factor models well explain the value-growth anomaly. Almost all of the alphas are indistinguishable from zero. The 3-Factor alpha of **cfp^{hl}** is 0.44% and has t -ratio 2.57 but it is no longer significant if we take into account of multiple testing. Meanwhile, its industry-adjusted version, **cfp_ia^{hl}**, has statistically significant 5-Factor alpha based on $CV(3, 5\%)$, but the profitability is mostly driven by micro-cap stocks. The Q-Factor model is also effective in capturing value-growth premium but seems to inflate the alphas of the portfolios with industry-adjusted firm characteristics. The portfolio mean return spreads of **bm_ia^{hl}** and **cfp_ia^{hl}** are insignificant in all types of stock universes, but their Q-Factor alphas turn significant in certain cases even after we adjust for data-snooping bias.

Momentum and volatility. The high-minus-low momentum and low-minus-high volatility portfolios are among the strategies that produce the greatest return spread in our sample of all stocks universe, Panels B and C of Table 3 summarize the results. The mean returns for long-short portfolios of **mom6^{hl}** (0.8%), **wh52^{hl}** (0.92%), **ma200^{hl}** (1.22%), **tvolf.d^{lh}** (0.82%), **tvolf.w^{lh}** (1%), and **ivolf.w^{lh}** (0.91%) are all above the non-studentized $CV(3, 5\%)$. However, the return spreads are sharply reduced and are no longer significant if we restrict the stocks to the all-but-tiny subsample. Moreover, the Q-Factor model shrinks all of the return spreads, with the exception of **ma200^{hl}**, into being insignificant in the all stock universe. The

Q-Factor alpha of $\mathbf{ma200}^{hl}$ becomes insignificant after we exclude the micro-cap stocks. The 4-Factor model works equally well in explaining momentum premium but fails to capture the return spreads in low volatility strategies.

Accrual, investment, and net share issues. Panel D of Table 3 summarizes the results for portfolios that are related to low growth anomaly. The t -ratios for mean returns of portfolios \mathbf{issue}^{lh} , $\mathbf{issue5}^{lh}$, and $\mathbf{grltnoa}^{lh}$ consistently surpass the $CV(2, 5\%)$ in the all and all-but-tiny stocks subsamples. However, only portfolio \mathbf{issue}^{lh} generates economically significant alpha in both universes. Nonetheless, as shown by Fama and French (2016) or Hou et al. (2015), the low growth anomalies may be explained by the investment factor in either 5-Factor or Q-Factor model, which is why the economic significance of \mathbf{issue}^{lh} disappears if we take risk-adjustment into consideration. For all types of risk-factor models, the portfolio alphas of \mathbf{acc}^{lh} in all stocks universe exceed the 1.96 critical value but are insignificant under the multiple testing framework. The low investment portfolios, $\mathbf{invest_TWX}^{lh}$, $\mathbf{invest_AG}^{lh}$, and $\mathbf{invest_LWZ}^{lh}$, earn positive premium, which is, however, insignificant with t -ratio below 1.96. The portfolio $\mathbf{invest_LWZ}^{lh}$ has surprisingly significant negative alpha in the all-but-tiny subsample once the investment factor is included in the risk adjustment.

Profitability. Panel E of Table 3 presents the results of the portfolios sorted by profitability factors. We find that none of the mean returns in this category is significant by any criteria. Although the portfolios based on improved profitability measures, such as Novy-Marx (2013)'s \mathbf{gpa}^{hl} and Ball et al. (2015)'s \mathbf{opa}^{hl} , have slightly greater mean returns than other profitability portfolios, they are still statistically and economically insignificant in our sample. The portfolio \mathbf{opa}^{hl} has significant risk-adjusted returns in all stocks universe but only when the CAPM or 3-Factor model is used. The portfolio \mathbf{opa}^{hl} generates 3-Factor alpha of 0.93% with t -ratio being 3.1, which exceed the corresponding studentized and non-studentized $CV(2, 5\%)$.

Illiquidity and trading activity. Panel F of Table 3 reports the results for portfolios that are constructed to earn the illiquidity premium. Our findings suggest that the best proxy for illiquidity premium is the portfolio \mathbf{illiq}^{hl} . Its studentized and non-studentized test statistics for mean returns are greater than the corresponding $CV(3, 5\%)$. The t -ratios of the alphas based on any risk factor models are also significant without data-snooping bias. However, the illiquidity premium in \mathbf{illiq}^{hl} would sharply disappear once the micro-cap stocks are excluded before portfolio sorts. Two of the trading activity portfolios (\mathbf{dvol}^{lh} , and $\mathbf{std_dvol}^{lh}$) by Chordia et al. (2001) generate modest mean returns and high t -ratios even in the case where we remove the micro-cap stocks, however they do not survive the test without multiple testing bias.

5 Monthly Rebalanced Portfolios

The profitability of some anomalies could be short-lived and may need rebalancing at monthly frequency. For example, one of the momentum strategies in Jegadeesh (1990) assumes one-month holding period. This subsection considers a universe where investors rebalance their portfolios at the end of every month. In this universe of monthly rebalanced portfolios, we use 45 predictors, where 34 of these are defined similarly to CRSP variables in the annual predictors. The additional 11 firm characteristics are computed with Compustat Quarterly. To ensure there is a large enough number of stocks to form portfolios in each decile group, the sample for monthly rebalanced portfolio returns starts from July 1978. We summarize the monthly predictors in Appendix B2.

Table 4 shows that the hurdle rates for t -ratios in the monthly rebalanced portfolios universe are lower than their annual counterpart. The cut-off points that control FWER(1), $CV(1, 5\%)$, to separate between superior and inferior portfolio strategies are approximately 2.93–3.19. The $CV(3, 5\%)$ ranges between 2.16 and 2.60. In contrast, the critical value for the non-studentized test statistics shown in Table 5 is generally greater than the annually rebalanced portfolio's. For instance, the $CV(3, 5\%)$ for mean return spread is 0.86% in the monthly rebalanced portfolios using all-but-tiny stocks, but the corresponding number in Table 2 shows 0.76%. This implies that the strategies under the null, i.e., the ones with less than zero actual mean returns, in the monthly rebalanced portfolios universe could produce greater portfolio returns. Intuitively, because there is a greater variation associated with higher turnover rate strategies, it should need a greater hurdle rate to justify the significance of the mean returns, and the resampling-based null distribution takes this effect into account. The critical values for the alphas of 5-Factor and Q-Factor model also increase. However, not all of the tests result in greater critical values, e.g., the multiple testing with CAPM and 3-Factor model.

Table 6 lists the portfolios with t -ratios of mean returns and Q-Factor's alphas exceeding their corresponding $CV(3, 5\%)$. After we exclude micro-cap stocks, 8 out of 44 anomalies are significant based on studentized test for the mean returns, and only 4 are with significant non-studentized test statistics. Similar to the annually rebalanced case, the high mean returns of low-minus-high volatility portfolios appear to be mostly attributed to micro-cap stocks. On the other hand, the momentum portfolios, such as **mom12^{hl}**, **mom712^{hl}**, and **mom12.ia^{hl}**, now perform better. The mean return spreads generated by **mom12^{hl}** (1.26%) and **mom712^{hl}** (1.24%) surpass the $CV(1, 5\%)$, but these are captured by the Q-Factor model. The only significant Q-Factor's alpha based on both studentized and non-studentized tests in all-but-tiny stocks universe is the short-term reversal strategy **ma20^{lh}**. The momen-

tum portfolio based on moving average **ma200^{hl}**, which works well with annual rebalancing frequency, does not generate significant returns.

6 Is the Error Rate Unduly Conservative?

This section discusses whether the multiple testing that controls FWER(3) is unduly strict so that our empirical results identify too few superior predictors. We also consider a simultaneous inference scenario where anomalies are classified into multiple families to see if the test could uncover more significant findings.

6.1 Controlling the False Discovery Proportion

The generalization of FWER(1) to FWER(k) helps increase the statistical power of multiple testing when the number of hypotheses becomes too large. In our empirical analysis, we choose 3 as the maximum of k as suggested by the simulation results of Romano and Wolf (2007) and Hsu et al. (2014). Further increasing the k may induce too many Type I errors in the process of identifying anomalies. However, there is also a concern that $k = 3$ is still unduly stringent, thus reducing the statistical power to detect superior cross-sectional stock return predictors.

Romano and Wolf (2007) provide a “data-driven” procedure on how to choose k by controlling the probability of false discovery proportion (FDP), the ratio between the number of false rejections and the number of total rejections, exceeding γ below δ ,

$$\text{FDX} \equiv \mathbb{P}\{\text{FDP} \geq \gamma\} \leq \delta. \quad (3)$$

Hsu et al. (2014) shows that the above inequality (3) is satisfied asymptotically by applying Step-SPA(k) algorithm until $k/(R_k + 1) > \gamma$, where R_k is the number of total rejections based on Step-SPA(k) test.

Table 7 presents the implied choice of k so that the probability of FDP exceeding γ is bounded below $\delta = 0.05$. Genovese and Wasserman (2006) shows that controlling FDP at (γ, δ) level implies the FDR, the expected value of FDP, is bounded below $\gamma + (1 - \gamma)\delta$. Therefore, FDR is also controlled at 0.0975 and 0.145 levels in the case of $\gamma = 0.05$ and $\gamma = 0.1$, respectively. To control FDR below 0.1 is widely accepted in the multiple testing literature and is also adopted by Harvey et al. (2016). In Table 7 the implied k never exceeds 3 except when testing the predictability using CAPM as the risk factor model. For the mean and Q-Factor alpha, the FDP controlling procedure implies that $k = 1$ is the appropriate

error rate in both studentized and non-studentized tests. The overall results suggest that controlling FWER(3) is not too stringent.

6.2 Selective inference

This subsection aims at an algorithm of constructing hierarchical hypotheses by taking the insights from financial theories. Namely, it aims at an alternative algorithm in contrast with conducting the multiple testing in the previous discussion, where we formulate the family-wise hypothesis under one question: “Is the cross-sectional stock return predictable?” To illustrate how an alternative algorithm works. Consider, for instance, that we first examine the hypothesis “Does valuation ratio (or momentum, growth, etc.) predict stock returns?”, and then perform multiple testing using the proxy variables for valuation ratio.

To accomplish this task, we adopt the selective inference procedure by Benjamini and Bogomolov (2014). Suppose the global family-wise hypothesis is classified into G multiple families. Let the mean exceedance FDP over the selected families be

$$\mathbb{E}^S[\text{FDX}] \equiv \mathbb{E} \left[\frac{1}{S_G} \sum_{g=1}^{S_G} \mathbb{1}\{\text{FDP}_g \geq \gamma\} \right] \leq \delta,$$

where S_G is the number of selected families and FDP_g is the FDP in group g . The Theorem 1 in Benjamini and Bogomolov (2014) proves that the following procedure controls $\mathbb{E}^S[\text{FDX}]$ at δ ,

1. Select the family if the maximum of the t -ratio in the family exceed 1.96.
2. For each selected family g , identify the superior strategies by conducting the multiple testing which controls

$$\mathbb{P}\{\text{FDP}_g \geq \gamma\} \leq \frac{S_G}{G} \delta.$$

For studentized and non-studentized tests, we apply the same selection rule in Step 1³. In Step 2, we use the same algorithm as in controlling the FDP in the Equation (3), only now the test is performed within an isolated group and with a significance level that is adjusted for selection effect.

Table 8 shows the multiple testing results using $\gamma = 0.1$ and $\delta = 0.05$. We use the same classification of predictors listed in Table 3 and categorize the rest of the predictors into “Others”. The total number of rejections may increase or decrease compared to the number

³The selection procedure in Step 1 could be based on Bonferroni procedure or other multiple testing procedure that satisfies the definition of simple selection procedure in Benjamini and Bogomolov (2014). Here we choose a less stringent criterion since one of our objectives in this subsection is to obtain a less conservative test.

of rejections by controlling FWER(3). For example, in the studentized test for all stocks universe the selective inference identifies 19 portfolios with significant mean returns, while the total number of rejections is 16 based on the test which controls FWER(3); however, the selective inference identifies fewer statistically significant predictors for the all-but-tiny stocks universe. We warn that the inference using multiple families does not guarantee the overall FWER(k) is still controlled. Nevertheless, the selective inference method is effective when we aim to label the predictors with certain types and conduct the multiple tests in two stages.

The selective inference procedure could lead to a different set of significant predictors. For example, the total number of significant Q-Factor alphas in the all stocks universe is 3 based on the studentized test statistics, which equals the number based on $CV(3, 5\%)$ (see Table 1). However, without separating the hypotheses into multiple families, **cfp_ia^{hl}**, **cashprod^{hl}**, and **illiq^{hl}** are the significant portfolios, while the selective inference identifies **cfp_ia^{hl}**, **ma200^{hl}**, and **illiq^{hl}** as the portfolios with significant Q-Factor alphas. Moreover, the selective inference procedure suggests that there are 6 economically significant portfolio mean returns from 3 different categories of firm characteristics in the all-but-tiny stocks universe. These portfolios are: **sp^{hl}**, **cfp^{hl}**, **mom6^{hl}**, **ma200^{hl}**, **issue^{lh}**, and **issue5^{lh}**. This is in contrast to the FWER(3) controlling procedure, which only identifies one economically significant portfolio (**issue^{lh}**). Another notable result is that none of the predictors in the “Others” category generate economically significant mean returns or Q-Factor alphas when tiny stocks are excluded before portfolio construction.

7 Data-Snooping Bias in the Pre-Fama and French (1993) Era

To distinguish between data-snooping bias and the post-publication effect documented by McLean and Pontiff (2016), we split the sample into pre- and post-1993 time periods. McLean and Pontiff (2016) show that many firm-characteristics lose their predictive power after the anomalies are made well-known by academic publications, and suggest that the role of arbitrage by sophisticated investors as the cause of disappearing anomalies. Since the publication of Fama and French (1993) should mark the beginning of active pieces of research work in cross-sectional stock return anomalies, we use the year 1993 as the approximate cut-off to investigate if the data-snooping bias is confounded by the post-publication effect.

Table 9 presents both pre- and post-1993 multiple testing results. In the pre-1993 sample period, studentized test shows a quite similar magnitude of data-snooping bias with the full sample analysis. For the all stocks universe, there are 44 portfolio mean returns with t -ratio above 1.96, but only 16 of those surpass $CV(3, 5\%)$. Compared to the results for the post-1993 period, the overall pieces of evidence for cross-sectional stock return predictability are

more pervasive in the pre-1993. With adjustment for data-snooping bias and exclusion of micro-cap stocks, both studentized and non-studentized tests show none of the predictors could successfully construct a profitable long-short portfolio returns in the post-1993 sample period. The critical values for non-studentized test statistics are substantially greater in the post-1993 sample period. The result appears to reinforce the findings that it becomes much harder to find consistently outperforming stock selection rules in the post-Fama and French (1993) era⁴.

Rolling subsample analysis. Instead of splitting the sample into two periods arbitrarily, we also examine how the predictive ability of the firm-characteristics evolves over time. As of the end of June each year, we use the data over the past 10 years to conduct the multiple testing. Figures 1 and 2 show the portfolios with studentized and non-studentized test statistics above $CV(3, 5\%)$ at the end of each vintage point, respectively. The results show that there remain fewer informative predictors in recent years. The findings are more pronounced using the all-but-tiny stocks universe⁵.

Panels A and B of Figure 1 show that the portfolios **illiq**^{hl}, **size**^{lh}, **mom12_ia**^{hl}, **tvol_w**^{hl}, and **issue5**^{lh} are among the most statistically significant anomalies in the subsample before year 1990. After the year 2000, the cross-section of stock returns are mostly predictable by less “popular” firm characteristics (e.g., **cashprod**^{lh}, **saleta**^{hl}, and **chceq**^{lh}). In the non-studentized test, the portfolio mean returns of **size**^{lh} and **bm**^{hl} are significant only for the periods before 1990. Between the vintage point from 1990 to 2000, low volatility and high momentum are the persistently profitable strategies. The evidence for cross-sectional stock return predictability barely exists in the most recent subsamples. Figure 2 also shows that the estimated $CV(3, 5\%)$ for non-studentized test using the sample period in the 2000’s increases, which resemble the findings in the pre- versus post-1993 comparison study.

8 Conclusion

This study investigates how the cross-sectional stock return predictors perform under the multiple testing method. We adopt firm characteristics from the empirical asset pricing literature and then form long-short portfolios to examine their profitability. The results show that most predictors lose their statistical significance once we adjust for data-snooping bias. Moreover, we find that the positive return spreads associated with some statistically significant anomalies are driven by micro-cap stocks. The pieces of evidence for economic significance are also

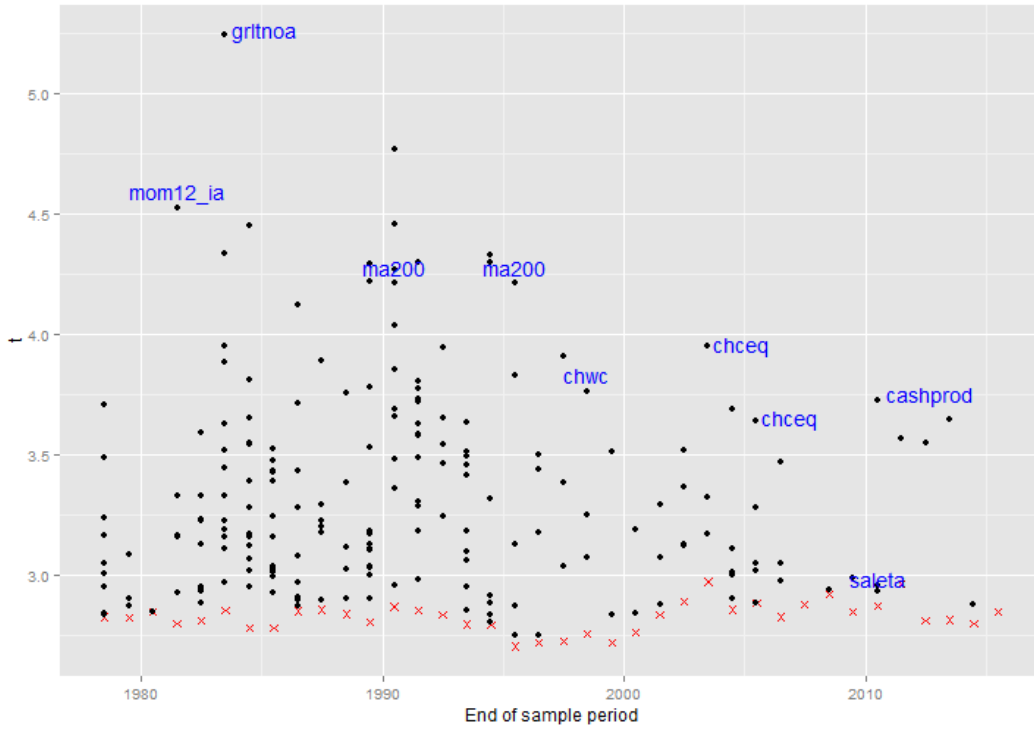
⁴The $CV(k, 5\%)$ is now greater due to the increasing variability of the k -th largest alpha.

⁵In the results not shown here, the analysis with Q-Factor model also confirms the pattern that the evidence for stock return predictability becomes weakened using the recent subsamples.

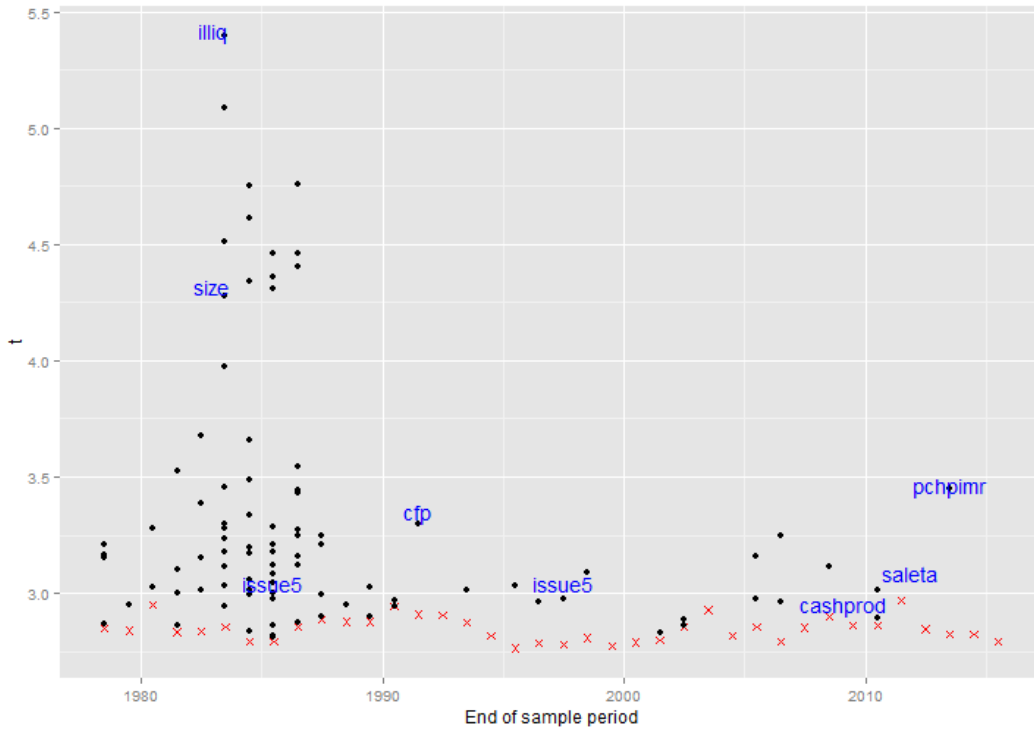
weak. For the annually rebalanced portfolios, the net share issues anomaly generates economically and statistically significant return premium, but it is well explained by 5-Factor or Q-Factor model. For the monthly rebalanced portfolios, only the short-term reversal strategy based on moving average delivers both economically and statistically significant mean return and Q-Factor alpha in the all-but-tiny stocks universe.

Under the selective inference with multiple families, we find more portfolios with economically significant mean returns than the multiple testing that controls the global error rate. Nevertheless, their risk-adjusted returns based on Q-Factor model do not surpass the corresponding critical values. Furthermore, our analyses with different subsamples suggest that the evidence for cross-sectional stock return predictability without data-snooping bias may be obtained mostly during the period before year 2000.

Figure 1: Studentized test with rolling subsamples.



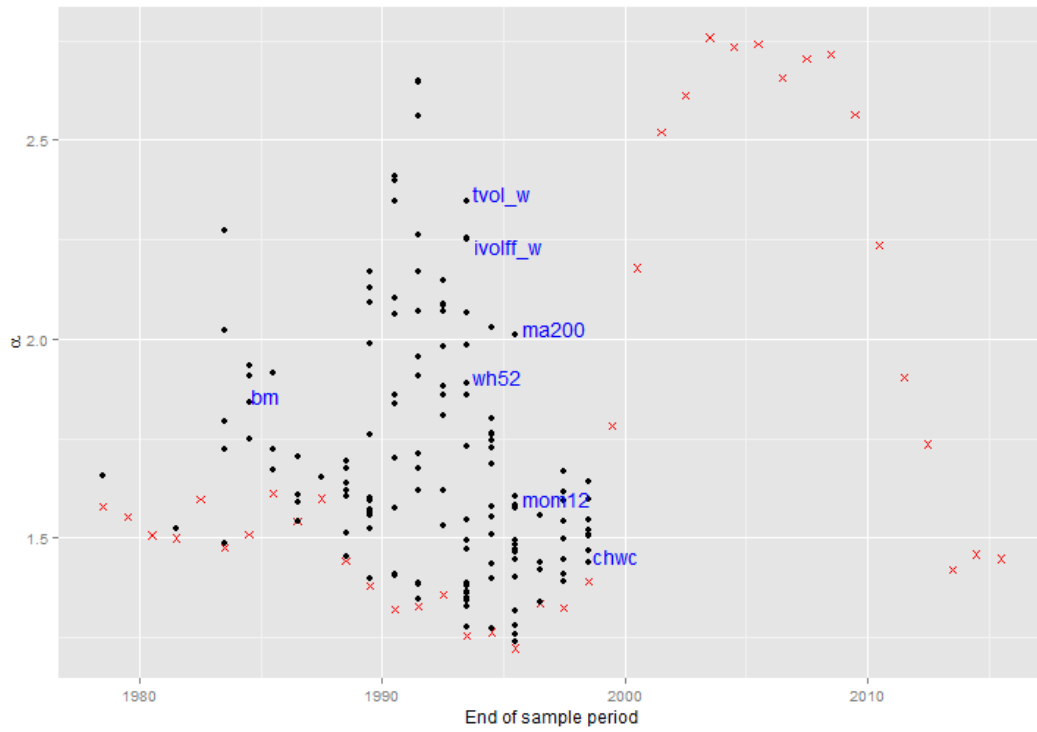
Panel A. All stocks universe



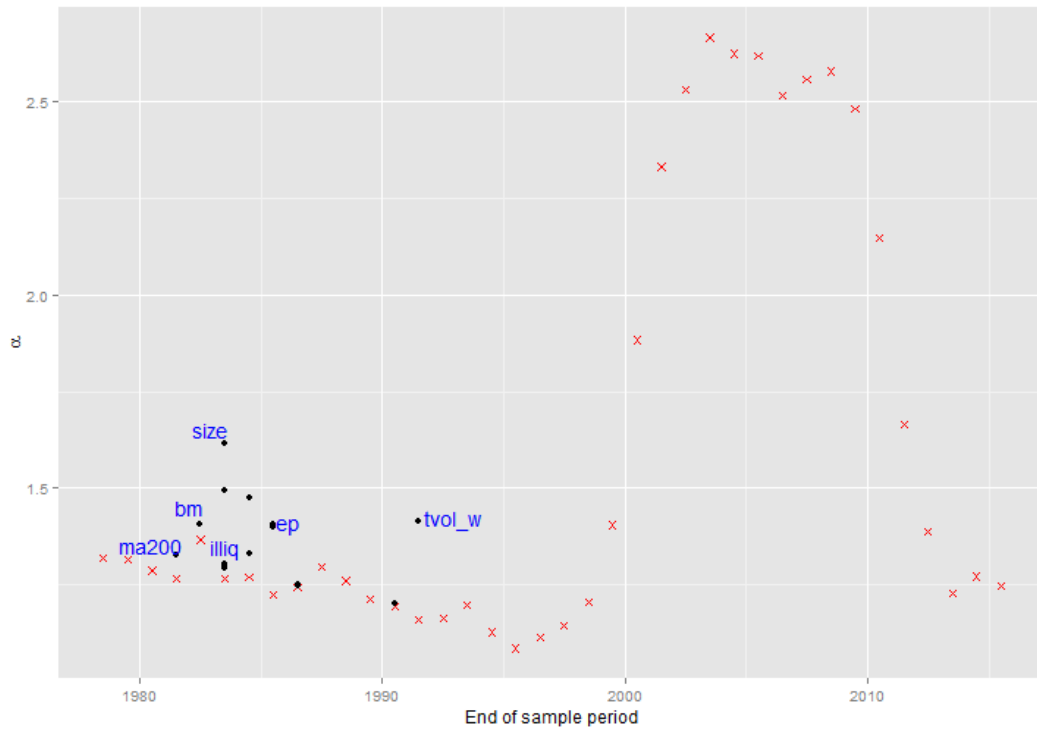
Panel B. All-but-tiny stocks universe

Note: The cross signs are the $CV(3,5\%)$ for the t -ratios estimated with the past 10-year subsamples. The y-axis and x-axis denote the t -ratios for the mean returns and ending time points of the subsamples, respectively.

Figure 2: Non-studentized test with rolling subsamples.



Panel A. All stocks universe



Panel B. All-but-tiny stocks universe

Note: The cross signs are the $CV(3,5\%)$ for the alphas estimated with the past 10-year subsamples. The y-axis and x-axis denote the mean returns and ending time points of the subsamples, respectively.

Table 1: The number of rejections based on t -ratios.

	FWER(1)	FWER(2)	FWER(3)	$t > 1.96$
Panel A. All stocks, long-short decile portfolios.				
Mean	9 (3.410)	15 (2.993)	16 (2.813)	41
CAPM	21 (3.423)	28 (2.995)	32 (2.747)	56
3-Factor	18 (3.456)	22 (3.012)	25 (2.782)	44
4-Factor	7 (3.452)	11 (3.017)	12 (2.799)	28
5-Factor	10 (3.472)	14 (3.022)	19 (2.800)	47
Q-Factor	0 (3.526)	3 (3.129)	3 (2.925)	19
Panel B. All stocks, long-short quintile portfolios.				
Mean	3 (3.378)	9 (3.016)	13 (2.839)	32
CAPM	18 (3.345)	23 (2.994)	29 (2.776)	57
3-Factor	14 (3.413)	18 (3.019)	22 (2.759)	49
4-Factor	3 (3.456)	6 (3.038)	9 (2.828)	21
5-Factor	15 (3.461)	18 (3.054)	21 (2.834)	47
Q-Factor	1 (3.448)	2 (3.127)	3 (2.912)	23
Panel C. All-but-tiny stocks, long-short decile portfolios.				
Mean	3 (3.490)	6 (3.102)	9 (2.879)	29
CAPM	10 (3.438)	16 (3.053)	19 (2.878)	49
3-Factor	6 (3.441)	10 (3.047)	13 (2.838)	38
4-Factor	1 (3.447)	1 (3.095)	2 (2.844)	12
5-Factor	10 (3.535)	16 (3.108)	20 (2.843)	39
Q-Factor	0 (3.516)	0 (3.103)	2 (2.898)	19
Panel D. Large-cap stocks, long-short decile portfolios.				
Mean	1 (3.464)	3 (3.127)	4 (2.908)	24
CAPM	3 (3.447)	6 (3.125)	8 (2.875)	36
3-Factor	5 (3.431)	7 (3.067)	8 (2.837)	24
4-Factor	1 (3.451)	1 (3.073)	2 (2.873)	9
5-Factor	9 (3.505)	14 (3.058)	18 (2.866)	38
Q-Factor	0 (3.456)	2 (3.103)	2 (2.942)	21

Note: The values in parentheses are the critical values $CV(k, 5\%)$ for the t -ratios, which are estimated so that $\text{FWER}(k)$, $k = 1, 2$, and 3 , is bounded below 5% level. To calculate the t -ratios, we use Newey-West standard error with lag parameter equaling 4. The row “Mean” reports the results for average portfolio returns without any risk adjustment. The “all-but-tiny” and “large-cap” stocks are those with market capitalization at the end of June greater than NYSE 20% and 50% quantiles, respectively.

Table 2: The number of rejections based on α 's critical value.

	FWER(1)	FWER(2)	FWER(3)
Panel A. All stocks, long-short decile portfolios.			
Mean	5 (0.944)	9 (0.845)	15 (0.781)
CAPM	18 (0.856)	24 (0.743)	29 (0.674)
3-Factor	20 (0.731)	20 (0.643)	23 (0.590)
4-Factor	7 (0.769)	14 (0.654)	15 (0.597)
5-Factor	11 (0.725)	13 (0.625)	18 (0.574)
Q-Factor	0 (0.978)	0 (0.878)	1 (0.819)
Panel B. All stocks, long-short quintile portfolios.			
Mean	0 (0.789)	0 (0.725)	3 (0.695)
CAPM	13 (0.701)	17 (0.627)	20 (0.581)
3-Factor	13 (0.612)	17 (0.531)	18 (0.491)
4-Factor	3 (0.628)	6 (0.552)	8 (0.509)
5-Factor	13 (0.573)	17 (0.486)	22 (0.429)
Q-Factor	1 (0.747)	2 (0.669)	3 (0.624)
Panel C. All-but-tiny stocks, long-short decile portfolios.			
Mean	0 (0.862)	1 (0.805)	1 (0.755)
CAPM	9 (0.798)	12 (0.740)	13 (0.684)
3-Factor	9 (0.685)	14 (0.585)	16 (0.550)
4-Factor	0 (0.691)	1 (0.610)	2 (0.564)
5-Factor	11 (0.674)	16 (0.570)	20 (0.507)
Q-Factor	0 (0.920)	1 (0.805)	1 (0.758)
Panel D. Large-cap stocks, long-short decile portfolios.			
Mean	0 (0.826)	0 (0.755)	1 (0.709)
CAPM	2 (0.795)	7 (0.721)	7 (0.669)
3-Factor	4 (0.670)	8 (0.580)	11 (0.533)
4-Factor	0 (0.666)	0 (0.584)	2 (0.547)
5-Factor	11 (0.646)	15 (0.546)	21 (0.496)
Q-Factor	0 (0.887)	0 (0.781)	1 (0.733)

Note: The values in parentheses are the critical values $CV(k, 5\%)$ for $\hat{\alpha}$, which are estimated so that $FWER(k)$, $k = 1, 2$, and 3 , is controlled below 5% level. The mean and risk-adjusted returns are in percentage. The “all-but-tiny” and “large-cap” stocks are those with market capitalization at the end of June greater than NYSE 20% and 50% quantiles, respectively.

Table 3: Selected anomalies.

		Mean		CAPM		3-Factor		4-Factor		5-Factor		Q-factor	
		α	t	α	t	α	t	α	t	α	t	α	t
Panel A. Value-growth anomaly.													
bm^{hl}	all stocks	0.90	3.31	0.93	3.31	0.26	1.66	0.27	1.71	0.25	1.54	0.41	1.78
	all-but-tiny	0.57	2.33	0.66	2.55	0.01	0.09	-0.04	-0.30	-0.04	-0.28	0.04	0.16
bm_ia^{hl}	all stocks	0.26	1.32	0.18	0.82	0.07	0.35	0.14	0.71	0.38	2.03	0.60	2.70
	all-but-tiny	0.22	1.16	0.17	0.82	0.13	0.68	0.14	0.72	0.47	2.43	0.62	2.91
cfp^{hl}	all stocks	0.42	1.52	0.61	2.45	0.34	1.55	0.27	1.24	0.08	0.36	0.13	0.49
	all-but-tiny	0.70	3.09	0.89	4.08	0.44	2.57	0.34	2.10	0.13	0.83	0.21	1.02
cfp_ia^{hl}	all stocks	0.44	2.06	0.41	1.77	0.39	1.89	0.37	1.74	0.59	2.88	0.76	3.14
	all-but-tiny	0.28	1.48	0.23	1.15	0.15	0.84	0.21	1.06	0.30	1.68	0.54	2.63
em^{lh}	all stocks	0.02	0.10	-0.06	-0.24	-0.16	-0.61	-0.26	-1.08	0.29	1.09	0.25	0.78
	all-but-tiny	0.41	1.84	0.39	1.70	0.13	0.59	0.02	0.09	0.48	2.01	0.65	2.36
ep^{hl}	all stocks	0.25	0.80	0.49	1.78	0.22	0.87	0.08	0.31	0.06	0.27	0.21	0.72
	all-but-tiny	0.44	1.78	0.61	2.54	0.20	1.02	0.09	0.44	0.04	0.20	0.23	0.98
sp^{hl}	all stocks	1.04	3.14	1.04	2.88	0.26	1.21	0.25	1.15	-0.12	-0.56	0.02	0.06
	all-but-tiny	0.71	2.42	0.75	2.31	0.01	0.07	-0.01	-0.07	-0.37	-2.00	-0.19	-0.67
Panel B. Momentum strategy.													
mom6^{hl}	all stocks	0.80	3.17	0.81	3.27	0.85	3.41	0.13	0.48	0.81	2.74	0.43	1.30
	all-but-tiny	0.66	2.84	0.60	2.66	0.62	2.60	-0.08	-0.35	0.57	1.96	0.15	0.45
mom12^{hl}	all stocks	0.71	2.35	0.79	2.52	1.09	4.14	0.39	1.45	0.91	3.39	0.50	1.59
	all-but-tiny	0.41	1.60	0.43	1.57	0.72	3.27	0.08	0.36	0.69	3.07	0.20	0.73
mom712^{hl}	all stocks	-0.14	-0.45	-0.08	-0.23	0.30	1.17	-0.03	-0.12	0.29	1.12	0.12	0.38
	all-but-tiny	-0.08	-0.29	-0.09	-0.31	0.32	1.42	-0.02	-0.07	0.37	1.66	0.04	0.14
mom12_ia^{hl}	all stocks	0.59	2.48	0.62	2.57	0.90	4.28	0.40	1.79	0.86	3.69	0.61	2.14
	all-but-tiny	0.45	2.22	0.42	1.93	0.70	3.85	0.26	1.36	0.79	4.02	0.54	2.17
mom12_ind^{hl}	all stocks	-0.03	-0.10	-0.04	-0.15	0.19	0.71	-0.35	-1.36	0.12	0.47	-0.26	-0.82
	all-but-tiny	0.03	0.13	0.02	0.08	0.18	0.80	-0.36	-1.57	0.06	0.24	-0.43	-1.39
wh52^{hl}	all stocks	0.92	2.68	1.27	4.49	1.39	5.58	0.64	2.33	0.94	3.55	0.50	1.70
	all-but-tiny	0.52	2.17	0.83	4.37	0.91	4.81	0.28	1.47	0.57	2.93	0.15	0.75
ma50^{hl}	all stocks	0.66	2.55	0.75	2.84	1.07	4.22	0.55	2.04	1.26	5.02	0.72	2.36
	all-but-tiny	0.40	1.60	0.42	1.62	0.76	3.28	0.28	1.35	1.09	4.70	0.61	1.89
ma100^{hl}	all stocks	1.09	4.56	1.21	5.19	1.41	5.51	0.74	2.47	1.31	4.41	0.70	2.11
	all-but-tiny	0.62	2.53	0.66	2.73	0.90	3.51	0.26	0.94	0.99	3.20	0.46	1.17
ma200^{hl}	all stocks	1.22	4.50	1.31	5.04	1.53	5.79	0.68	2.32	1.42	4.65	0.84	2.53
	all-but-tiny	0.67	2.52	0.68	2.52	0.99	3.86	0.22	0.86	1.04	3.70	0.42	1.19
Panel C. Low volatility strategy.													
tvolf_d^{lh}	all stocks	0.82	2.14	1.25	4.16	1.16	4.32	0.96	3.47	0.51	2.04	0.41	1.34
	all-but-tiny	0.33	1.01	0.79	3.20	0.54	2.70	0.37	1.84	0.00	0.02	-0.01	-0.06
tvolf_w^{lh}	all stocks	1.00	2.28	1.50	4.44	1.33	4.85	1.16	4.21	0.62	2.78	0.67	2.07
	all-but-tiny	0.42	1.14	0.96	3.39	0.67	3.08	0.49	2.19	0.10	0.53	0.20	0.77
ivolf_d^{lh}	all stocks	0.72	2.19	1.07	3.88	1.03	4.73	0.83	3.40	0.39	1.96	0.25	1.05
	all-but-tiny	0.17	0.55	0.54	2.29	0.35	1.77	0.25	1.31	-0.11	-0.69	-0.14	-0.61
ivolf_w^{lh}	all stocks	0.91	2.27	1.31	4.02	1.22	4.56	1.06	3.89	0.55	2.35	0.58	1.88
	all-but-tiny	0.23	0.70	0.65	2.58	0.45	2.22	0.32	1.60	-0.07	-0.42	0.03	0.13

Table 3 (Continued): Selected anomalies.

		Mean		CAPM		3-Factor		4-Factor		5-Factor		Q-factor	
		α	t	α	t	α	t	α	t	α	t	α	t
ivolcapm_d^{lh}	all stocks	0.83	2.43	1.19	4.21	1.15	4.94	0.98	3.83	0.53	2.69	0.44	1.84
	all-but-tiny	0.13	0.45	0.51	2.16	0.31	1.58	0.24	1.21	-0.15	-0.88	-0.14	-0.60
ivolcapm_w^{lh}	all stocks	0.81	2.00	1.22	3.74	1.13	4.20	1.01	3.83	0.45	1.97	0.50	1.63
	all-but-tiny	0.33	1.01	0.78	3.07	0.57	2.74	0.43	2.11	0.00	0.01	0.10	0.41
beta^{lh}	all stocks	0.15	0.49	0.65	2.64	0.39	1.69	0.11	0.44	-0.07	-0.30	-0.22	-0.79
	all-but-tiny	0.33	1.03	0.86	3.36	0.56	2.69	0.31	1.41	0.04	0.19	-0.01	-0.03
Panel D. Growth-related anomaly.													
invest_TWX^{lh}	all stocks	0.23	1.22	0.18	0.97	0.22	1.22	0.05	0.25	0.28	1.53	0.15	0.71
	all-but-tiny	0.26	1.49	0.27	1.48	0.33	1.92	0.13	0.74	0.31	1.82	0.09	0.44
invest_AG^{lh}	all stocks	0.29	1.44	0.41	2.13	0.23	1.15	0.19	0.91	0.01	0.05	-0.12	-0.45
	all-but-tiny	0.26	1.30	0.39	2.11	0.20	1.10	0.11	0.62	-0.14	-0.85	-0.34	-1.69
invest_LWZ^{lh}	all stocks	0.40	1.30	0.67	2.17	0.06	0.25	-0.12	-0.53	-0.61	-3.14	-0.69	-2.32
	all-but-tiny	0.38	1.19	0.65	2.07	0.05	0.22	-0.17	-0.79	-0.69	-3.49	-0.82	-2.75
agr^{lh}	all stocks	0.80	3.49	0.95	3.83	0.52	2.97	0.38	2.10	0.02	0.13	-0.08	-0.39
	all-but-tiny	0.63	2.74	0.81	3.34	0.40	2.42	0.32	2.04	-0.18	-1.29	-0.24	-1.32
issue^{lh}	all stocks	0.89	3.77	1.06	4.54	0.82	4.31	0.75	4.03	0.30	1.96	0.26	1.31
	all-but-tiny	0.83	3.61	0.95	3.98	0.73	4.13	0.66	3.82	0.23	1.65	0.16	0.87
issue5^{lh}	all stocks	0.71	3.48	0.83	4.39	0.81	4.02	0.71	3.33	0.37	2.22	0.33	1.51
	all-but-tiny	0.71	3.65	0.84	4.44	0.75	3.89	0.60	3.09	0.31	2.01	0.30	1.57
acc^{lh}	all stocks	0.43	2.19	0.52	2.60	0.51	2.62	0.46	2.13	0.51	2.58	0.52	2.34
	all-but-tiny	0.31	1.89	0.36	2.26	0.34	2.05	0.25	1.40	0.29	1.81	0.31	1.67
grltnoa^{lh}	all stocks	0.73	4.86	0.78	4.94	0.59	4.07	0.51	3.11	0.24	1.63	0.08	0.47
	all-but-tiny	0.52	3.30	0.59	3.51	0.45	2.94	0.39	2.39	0.08	0.56	-0.10	-0.59
Panel E. Profitability.													
gpa^{hl}	all stocks	0.25	0.99	0.41	1.61	0.41	1.72	0.28	1.21	-0.39	-2.33	-0.52	-2.33
	all-but-tiny	0.28	1.37	0.36	1.58	0.40	2.07	0.28	1.45	-0.31	-1.87	-0.44	-2.05
gpa_ia^{hl}	all stocks	0.23	0.97	0.44	1.92	0.47	2.24	0.39	1.92	0.02	0.14	-0.04	-0.20
	all-but-tiny	0.13	0.64	0.34	1.61	0.36	1.96	0.27	1.53	-0.05	-0.30	-0.12	-0.65
opa^{hl}	all stocks	0.59	1.73	0.87	2.86	0.93	3.10	0.78	2.61	0.14	0.47	0.01	0.02
	all-but-tiny	0.34	1.35	0.52	2.04	0.62	2.67	0.44	1.83	-0.12	-0.66	-0.35	-1.47
gmr^{hl}	all stocks	0.07	0.28	0.28	1.21	0.33	1.51	0.30	1.47	-0.07	-0.39	-0.04	-0.16
	all-but-tiny	0.14	0.71	0.30	1.67	0.44	2.57	0.42	2.61	0.15	1.01	0.20	1.14
roe^{hl}	all stocks	0.11	0.37	0.35	1.28	0.43	1.73	0.26	1.09	-0.21	-1.02	-0.28	-1.09
	all-but-tiny	-0.08	-0.31	0.11	0.41	0.15	0.60	0.07	0.30	-0.47	-2.28	-0.53	-1.91
roa^{hl}	all stocks	0.19	0.54	0.49	1.60	0.48	1.74	0.38	1.34	-0.26	-1.14	-0.25	-0.81
	all-but-tiny	-0.04	-0.16	0.19	0.75	0.23	0.95	0.13	0.55	-0.41	-2.07	-0.46	-1.79
roic^{hl}	all stocks	0.29	0.89	0.57	1.88	0.49	1.80	0.56	2.12	-0.12	-0.59	0.00	0.02
	all-but-tiny	0.04	0.16	0.25	0.99	0.29	1.23	0.17	0.73	-0.34	-1.76	-0.44	-1.86

Table 3 (Continued): Selected anomalies.

		Mean		CAPM		3-Factor		4-Factor		5-Factor		Q-factor	
		α	t	α	t	α	t	α	t	α	t	α	t
Panel F. Illiquidity and trading activity.													
illiq^{hl}	all stocks	0.81	3.82	0.82	3.88	0.62	4.52	0.54	3.86	0.65	4.36	0.57	3.44
	all-but-tiny	0.30	2.29	0.28	2.16	0.08	0.87	0.05	0.53	0.06	0.67	-0.06	-0.54
turn^{lh}	all stocks	0.20	0.68	0.59	2.32	0.20	1.00	0.13	0.67	-0.22	-1.07	-0.23	-0.80
	all-but-tiny	0.19	0.60	0.62	2.39	0.25	1.19	0.16	0.77	-0.26	-1.31	-0.25	-0.87
std_turn^{lh}	all stocks	0.15	0.52	0.55	2.31	0.30	1.53	0.18	0.96	-0.17	-0.93	-0.19	-0.76
	all-but-tiny	0.08	0.27	0.46	1.99	0.21	1.10	0.09	0.50	-0.29	-1.62	-0.25	-1.06
dvol^{lh}	all stocks	0.31	1.71	0.43	2.24	0.15	1.26	0.15	1.29	0.14	1.20	0.15	1.05
	all-but-tiny	0.34	2.55	0.40	2.98	0.14	1.79	0.13	1.64	0.07	0.96	0.03	0.23
std_dvol^{lh}	all stocks	0.39	2.43	0.54	3.24	0.29	2.70	0.24	2.26	0.24	2.22	0.23	1.61
	all-but-tiny	0.33	2.34	0.43	3.04	0.15	1.67	0.09	1.01	0.05	0.62	0.00	0.04
zerotrade^{hl}	all stocks	0.41	1.45	0.86	3.49	0.45	2.26	0.36	1.92	0.02	0.10	0.02	0.07
	all-but-tiny	0.21	0.71	0.61	2.37	0.23	1.05	0.11	0.52	-0.31	-1.62	-0.33	-1.22
to12^{hl}	all stocks	0.25	0.79	0.68	2.64	0.32	1.56	0.24	1.18	-0.12	-0.61	-0.07	-0.24
	all-but-tiny	0.12	0.37	0.57	2.11	0.19	0.89	0.09	0.40	-0.32	-1.56	-0.23	-0.78

Table 4: Studentized multiple testing with monthly rebalanced portfolios.

	FWER(1)	FWER(2)	FWER(3)	$t > 1.96$
Panel A. All stocks, long-short decile portfolios.				
Mean	10 (3.063)	15 (2.660)	19 (2.444)	24
CAPM	23 (2.929)	23 (2.523)	29 (2.185)	32
3-Factor	22 (3.004)	27 (2.501)	28 (2.193)	29
4-Factor	17 (3.029)	19 (2.592)	22 (2.294)	25
5-Factor	14 (3.148)	18 (2.700)	19 (2.428)	26
Q-Factor	2 (3.068)	4 (2.767)	12 (2.476)	14
Panel B. All-but-tiny stocks, long-short decile portfolios.				
Mean	4 (3.047)	7 (2.757)	8 (2.499)	17
CAPM	17 (3.080)	24 (2.624)	25 (2.340)	27
3-Factor	21 (3.012)	22 (2.596)	25 (2.311)	27
4-Factor	5 (3.128)	9 (2.679)	13 (2.365)	19
5-Factor	4 (3.191)	7 (2.823)	9 (2.580)	15
Q-Factor	1 (3.106)	3 (2.808)	3 (2.596)	4

Note: See Table 1's note.

Table 5: Non-studentized multiple testing with monthly rebalanced portfolios.

	FWER(1)	FWER(2)	FWER(3)
Panel A. All stocks, long-short decile portfolios.			
Mean	11 (1.098)	15 (0.876)	17 (0.767)
CAPM	19 (0.849)	23 (0.679)	29 (0.530)
3-Factor	18 (0.760)	20 (0.614)	28 (0.493)
4-Factor	16 (0.767)	17 (0.631)	17 (0.549)
5-Factor	6 (1.097)	10 (0.960)	13 (0.837)
Q-Factor	0 (1.264)	1 (1.113)	3 (1.019)
Panel B. All-but-tiny stocks, long-short decile portfolios.			
Mean	2 (0.988)	3 (0.896)	4 (0.857)
CAPM	16 (0.815)	19 (0.684)	20 (0.616)
3-Factor	17 (0.735)	20 (0.612)	20 (0.544)
4-Factor	3 (0.759)	11 (0.644)	15 (0.551)
5-Factor	3 (0.971)	4 (0.869)	5 (0.790)
Q-Factor	0 (1.135)	1 (1.025)	1 (0.954)

Note: See Table 2's note.

Table 6: Monthly rebalanced portfolios with t -ratios greater than $CV(3, 5\%)$.

Panel A. All stocks, mean return spread.							
	abr^{hl}	mom712^{hl}	ma20^{lh}	mom12^{hl}	mom12_ia^{hl}	mom6^{hl}	ivolff_d^{lh}
α	1.187	1.615	0.993	1.915	1.290	1.361	1.469
t	6.747	5.237	4.664	4.432	3.632	3.553	3.527
	ivolcapm_d^{lh}	sue^{hl}	illiq^{hl}	tvolf_d^{lh}	roaq1^{hl}	roaq2^{hl}	roaq3^{hl}
α	1.404	0.441	0.713	1.446	0.816	0.790	0.928
t	3.527	3.208	3.161	3.101	2.992	2.867	2.814
	tvolf_w^{lh}	ivolff_w^{lh}	taxmom^{hl}	maxret^{lh}	ivolcapm_w^{lh}		
α	1.357	1.287	0.423	1.006	1.217		
t	2.680	2.648	2.623	2.594	2.516		
Panel B. All-but-tiny stocks, mean return spread.							
	abr^{hl}	ma20^{lh}	mom712^{hl}	mom12^{hl}	sue^{hl}	illiq^{hl}	mom12_ia^{hl}
α	0.764	0.860	1.241	1.259	0.434	0.453	0.928
t	4.690	4.663	4.136	3.584	2.997	2.996	2.950
	mom6^{hl}						
α	0.842						
t	2.631						
Panel C. All stocks, Q-Factor alpha.							
	abr^{hl}	ma20^{lh}	tvolf_w^{lh}	ivolff_d^{lh}	mom712^{hl}	illiq^{hl}	size^{lh}
α	1.103	1.182	0.939	0.939	0.941	0.464	1.035
t	5.225	4.155	2.916	2.815	2.755	2.707	2.697
	ivolcapm_w^{lh}	tvolf_d^{lh}	ivolff_w^{lh}	accq^{lh}	season^{hl}		
α	0.832	0.901	0.815	0.436	0.546		
t	2.670	2.654	2.559	2.515	2.508		
Panel D. All-but-tiny stocks, Q-Factor alpha.							
	ma20^{lh}	abr^{lh}	season^{hl}				
α	1.079	0.597	0.514				
t	4.248	2.882	2.825				

Table 7: The choice of k by controlling FDP.

		Mean	CAPM	3-Factor	4-Factor	5-Factor	Q-Factor
Panel A. Studentized test.							
All stocks	$\gamma = 0.05$	1	2	1	1	1	1
	$\gamma = 0.1$	2	4	3	1	2	1
All-but-tiny stocks	$\gamma = 0.05$	1	1	1	1	1	1
	$\gamma = 0.1$	1	2	1	1	2	1
Panel B. Non-studentized test.							
All stocks	$\gamma = 0.05$	1	1	2	1	1	1
	$\gamma = 0.1$	1	4	3	1	2	1
All-but-tiny stocks	$\gamma = 0.05$	1	1	1	1	1	1
	$\gamma = 0.1$	1	2	2	1	2	1

Note: This table reports the choice of k in $\text{FWER}(k)$ by controlling the probability of FDP exceeding γ to be below 5%.

Table 8: Selective inference with multiple families.

	Studentized		Non-studentized	
	Mean	Q-Factor	Mean	Q-Factor
Panel A. All stocks.				
Value	2 (2.618)	1 (2.710)	2 (0.713)	0 (0.794)
Momentum	7 (2.104)	1 (2.472)	6 (0.626)	1 (0.774)
Volatility	3 (2.246)	0 (2.552)	6 (0.617)	0 (0.749)
Growth	4 (2.440)	0 (2.653)	4 (0.636)	1 (0.573)
Profitability	#	0 (2.633)	#	0 (0.759)
Trading	1 (2.619)	1 (2.549)	1 (0.707)	0 (0.647)
Others	2 (3.363)	0 (3.407)	1 (0.920)	0 (0.904)
Total	19	3	20	2
Panel B. All-but-tiny stocks.				
Value	1 (2.806)	1 (2.843)	2 (0.625)	0 (0.709)
Momentum	1 (2.570)	0 (2.730)	2 (0.639)	0 (0.895)
Volatility	#	#	#	#
Growth	4 (2.528)	0 (2.771)	2 (0.668)	1 (0.524)
Profitability	#	0 (2.709)	#	0 (0.652)
Trading	0 (2.602)	#	0 (0.717)	#
Others	0 (3.527)	0 (3.514)	0 (0.869)	0 (0.874)
Total	6	1	6	1

Note: This table reports the number of rejections and its critical value in parentheses when the average of exceedance FDP over the selected families is controlled at 5% significance level. We choose the exceedance level of FDP to be 0.1. The symbol # indicates that the family is not selected because its maximum t -ratio is below 1.96.

Table 9: Multiple testing using pre- and post-1993 sample periods.

		All stocks		All-but-tiny stocks	
		Mean	Q-Factor	Mean	Q-Factor
Panel A. Studentized test.					
Pre-1993	FWER(1)	7 (3.331)	7 (3.491)	2 (3.359)	3 (3.497)
	FWER(2)	13 (2.935)	8 (3.089)	7 (3.021)	3 (3.102)
	FWER(3)	16 (2.744)	9 (2.871)	12 (2.783)	7 (2.910)
	$t > 1.96$	44	25	36	29
Post-1993	FWER(1)	0 (3.381)	0 (3.458)	0 (3.372)	0 (3.444)
	FWER(2)	2 (3.073)	1 (3.026)	0 (3.041)	0 (3.041)
	FWER(3)	2 (2.861)	1 (2.843)	0 (2.880)	0 (2.855)
	$t > 1.96$	12	6	9	8
Panel B. Non-studentized test.					
Pre-1993	FWER(1)	8 (1.121)	8 (1.084)	0 (0.947)	1 (1.009)
	FWER(2)	13 (0.968)	10 (0.937)	1 (0.842)	1 (0.865)
	FWER(3)	16 (0.893)	11 (0.850)	2 (0.792)	6 (0.777)
Post-1993	FWER(1)	0 (1.592)	0 (1.398)	0 (1.451)	0 (1.356)
	FWER(2)	0 (1.440)	0 (1.259)	0 (1.355)	0 (1.212)
	FWER(3)	0 (1.381)	0 (1.185)	0 (1.293)	0 (1.138)

Note: The pre-1993 and post-1993 results correspond to the multiple testing using the sample periods before and after the end of June 1993, respectively.

A Step-SPA(k) algorithm

This appendix illustrates the Step-SPA(k) algorithm that controls the k -family-wise error rate (FWER(k)) asymptotically. The key assumptions made by Step-SPA(k) algorithm are: (i) the parameters vector $\{\hat{\alpha}_1, \dots, \hat{\alpha}_M\}$ converges to multivariate normal distribution, and (ii) this asymptotic distribution can well be approximated by bootstrap simulation. We refer to Hsu et al. (2014) for further technical details and proofs.

Let $\hat{\alpha}_l$ denote the parameter of a portfolio $l \in \{1, \dots, M\}$ estimated from a time-series sample of size T . The null hypotheses are $H_0^l : \alpha_l \leq 0$, $l = 1, \dots, M$. We use the notation $k\text{-max}\{x_l; l \in A\}$ to denote k -th largest value of x in the subset $A \subseteq \{1, \dots, M\}$. The following algorithm can be used to asymptotically control FWER(k) below a threshold level δ .

Step-SPA(k) algorithm

(S1) Run the regression

$$R_{lt} = \alpha_l + \mathbf{F}_t' \beta_l + \varepsilon_{lt},$$

where \mathbf{F}_t is the vector of factor portfolio returns. To conduct multiple testing on the simple average returns, discard the $\mathbf{F}_t' \beta_l$.

(S2) Compute the studentized or non-studentized test statistics for each portfolio

$$\hat{d}_l = \sqrt{T} \frac{\hat{\alpha}_l}{\hat{\sigma}_l} \quad \text{or} \quad \sqrt{T} \hat{\alpha}_l,$$

where $\hat{\sigma}_l$ is the consistent estimator of $\hat{\alpha}_l$'s standard deviation.

(S3) Compute the re-centering estimators

$$\hat{\alpha}_l^- = \hat{\alpha}_l \cdot \mathbb{1} \left(\sqrt{T} \hat{\alpha}_l \leq -\hat{\sigma}_l \sqrt{2 \log \log T} \right),$$

where $\mathbb{1}$ is an indicator function.

(S4) For each bootstrap sample $b = \{1, \dots, B\}$, calculate the studentized or non-studentized bootstrap statistics

$$\hat{d}_l^b = \sqrt{T} \frac{\hat{\alpha}_l^b - \hat{\alpha}_l + \hat{\alpha}_l^-}{\hat{\sigma}_l} \quad \text{or} \quad \sqrt{T} (\hat{\alpha}_l^b - \hat{\alpha}_l + \hat{\alpha}_l^-),$$

where $\hat{\alpha}_l^b$ is the estimator of α_l using bootstrap sample b .

(S5) In each bootstrap sample, find $k\text{-max}\{\hat{d}_l^b; l \in A_1\}$, where $A_1 = \{1, \dots, M\}$.

(S6) Define $\hat{q}(1-\delta, k, A_1) = \max\{\tilde{q}(1-\delta, k, A_1), 0\}$, where $\tilde{q}(1-\delta, k, A_1)$ is the $(1-\delta)$ empirical quantile of the B values $k\text{-max}\{\hat{d}_l^1; l \in A_1\}, \dots, k\text{-max}\{\hat{d}_l^B; l \in A_1\}$.

(S7) (a) If $\max\{\hat{d}_l; l \in A_1\} \leq \hat{q}(1-\delta, k, A_1)$, then accept all null hypotheses and stop.

(b) If $\hat{d}_l > \hat{q}(1-\delta, k, A_1)$, then reject H_0^l .

(S8) Denote the collection of the index of the rejected hypotheses and the remaining hypotheses from the previous step by R_2 and A_2 , respectively.

(a) If $|R_2| < k$, then stop.

(b) If $|R_2| \geq k$, then find the new critical value as follows

$$\hat{c}(1 - \delta, k, A_2) = \max_{I \subset R_2, |I|=k-1} \{\hat{q}(1 - \delta, k, J); J = A_2 \cup I\},$$

where $|A|$ denotes the number of elements in set A and $\hat{q}(1 - \delta, k, J)$ is calculated as in the step (S5).

(S9) (a) If $\max\{\hat{d}_l; l \in A_2\} \leq \hat{c}(1 - \delta, k, A_2)$, then there is no further rejection, stop.

(b) If $\hat{d}_l > \hat{c}(1 - \delta, k, A_2)$ with $l \in A_2$, then reject H_0^l and go back to step (S7) by replacing R_2 and A_2 with R_j and A_j , $j \geq 3$.

For the studentized test, we use Newey-West standard error with lag parameter equaling 4 to estimate σ_l . To generate the bootstrap sample in Step (S4), we employ the stationary bootstrap procedure by Politis and Romano (1994), which re-samples the original data in blocks to capture the time-series dependence structure. Specifically, a bootstrap sample b is a set of random index obtained by the following algorithm.

Stationary bootstrap algorithm

(B1) Generate a random integer t_1^b which is uniformly distributed between 1 and T .

(B2) With probability Q , set $t_2^b = t_1^b + 1$, and with probability $1 - Q$, t_2^b is obtained by generating random interger between 1 and T .

(B3) Repeat step (B2) until the b -th bootstrap sample has T observations.

Politis and Romano (1994) show that the block size from the above algorithm follows a geometric distribution with parameter Q . In our empirical analysis, we use $Q = 0.8$, so that the expected block size is 5. We set the number of bootstrap replications $B = 2,000$.

B Predictor Definition

B.1 Annual Predictors

Table B1: Annual predictor definition

Variable	Reference	Definition
absacc	Bandyopadhyay et al. (2010)	$\text{abs}(\mathbf{acc})$
acc	Sloan (1996)	$(\Delta\{(\text{ACT} - \text{CHE}) - (\text{LCT} - \text{DLC} - \text{TXP})\} - \text{DP}) / \text{avg2}(\text{AT})$
agr	Cooper et al. (2008)	$\text{AT} / \text{lag1}(\text{AT}) - 1$
ato	Soliman (2008)	$\text{SALE} / \text{avg2}(\mathbf{noa})$
bas12	Liu (2006)	The average of daily $(\text{ASKHI} - \text{BIDLO}) / (\text{ASKHI} + \text{BIDLO})/2$ over the past 12 months.
beta	Fama and MacBeth (1973)	The beta coefficient of CAPM using weekly returns data over the past 52 weeks.
bm	Stattman (1980)	$(\text{SEQ} + \text{TXDB} + \text{ITCB} - \text{pref}) / (\text{PRCC_F} \times \text{CSHO})^a$
bm_ia	Asness et al. (2000)	$\mathbf{bm} - \text{IndMean}(\mathbf{bm})$
cash	Palazzo (2012)	CHE / AT
cashprod	Chandrashekar and Rao (2009)	$(\text{PRCC_F} \times \text{CSHO} + \text{DT} - \text{AT}) / \text{CHE}$
cfodebt	Ou and Penman (1989)	$\text{OANCF} / \text{avg2}(\text{DT})^b$
cfp	Desai et al. (2004)	$\text{OANCF} / (\text{PRCC_F} \times \text{CSHO})$
cfp_ia	Asness et al. (2000)	$\mathbf{cfp} - \text{IndMean}(\mathbf{cfp})$
chato	Soliman (2008)	$\Delta\{\text{SALE} / \text{avg2}(\mathbf{noa})\}$
chato_ia	Soliman (2004)	$\mathbf{chato} - \text{IndMean}(\mathbf{chato})$
chceq	Richardson et al. (2005)	$\Delta\text{CEQ} / \text{avg2}(\text{AT})$
chdiv	Ou and Penman (1989)	ΔDVT
chemp	Belo et al. (2014)	$\Delta\text{EMP} / \text{avg2}(\text{EMP})$
chemp_ia	Asness et al. (2000)	$\mathbf{chemp} - \text{IndMean}(\mathbf{chemp})$
chfin	Richardson et al. (2005)	$\Delta\{(\text{IVST} + \text{IVAO}) - (\text{DLTT} + \text{DLC} + \text{PSTK})\} / \text{avg2}(\text{AT})$
chinv	Thomas and Zhang (2002)	$\Delta\text{INVT} / \text{avg2}(\text{AT})$
chmom	Gettleman and Marks (2006)	$\mathbf{mom1} \times \mathbf{mom6} - \mathbf{mom712}$
chnco	Richardson et al. (2005)	$\Delta\{(\text{AT} - \text{ACT} - \text{IVAO}) - (\text{LT} - \text{LCT} - \text{DLTT})\} / \text{avg2}(\text{AT})$
chpm	Soliman (2008)	$\Delta\{\text{OIADP} / \text{SALE}\}$
chpm_ia	Soliman (2004)	$\mathbf{chpm} - \text{IndMean}(\mathbf{chpm})$
chrnoa	Soliman (2008)	$\Delta\{\text{OIADP} / \text{avg2}(\mathbf{noa})\}$
chrnoa_ia	Soliman (2004)	$\mathbf{chrnoa} - \text{IndMean}(\mathbf{chrnoa})$
chroe	Ou and Penman (1989)	$\Delta\mathbf{roe}$
chwc	Richardson et al. (2005)	$\Delta\{(\text{ACT} - \text{CHE}) - (\text{LCT} - \text{DLC})\} / \text{avg2}(\text{AT})$
currat	Ou and Penman (1989)	ACT / LCT
debteq	Ou and Penman (1989)	$\text{LT} / (\text{AT} - \text{LT})$
deprppe	Ou and Penman (1989)	DP / PPEGT
dvpl	Chordia et al. (2001)	$\log(\text{lag2}(\text{PRC} \times \text{VOL}))$
dy	Ball (1978)	$\text{DVT} / (\text{PRCC_F} \times \text{CSHO})$
em	Loughran and Wellman (2011)	$(\text{PRCC_F} \times \text{CSHO} + \text{DLC} + \text{DLTT} - \text{pref} - \text{CHE}) / \text{OIBDP}$
ep	Basu (1983)	$\text{IB} / (\text{PRCC_F} \times \text{CSHO})$
gmr	Ou and Penman (1989)	$(\text{SALE} - \text{COGS}) / \text{SALE}$
gpa	Novy-Marx (2013)	$(\text{SALE} - \text{COGS}) / \text{AT}$
gpa_ia	Novy-Marx (2013)	$\mathbf{gpa} - \text{IndMean}(\mathbf{gpa})$
grltnoa	Fairfield et al. (2003)	$\Delta\mathbf{noa} / \text{avg2}(\text{AT}) - \mathbf{acc}$
herf	Hou and Robinson (2006)	Herfindahl index, $\text{IndSum}(\{\text{SALE} / \text{IndSum}(\text{SALE})\}^2)$

Table B1 (Continued): Annual predictor definition

Variable	Reference	Definition
illiq	Amihud (2002)	The average of daily $\text{abs}(\text{RET})/(\text{PRC} \times \text{VOL})$ over the past 12 months.
invest_LWZ	Liu et al. (2009)	$(\text{CAPX} - \text{SPPE}) / \text{PPEGT}$
invest_TWX	Titman et al. (2004)	$(\text{CAPX}/\text{SALE}) / \text{lag1}(\text{avg3}(\text{CAPX}/\text{SALE})) - 1$
invest_AG	Anderson and Garcia-Feijóo (2006)	$(\text{lag1}(\text{CAPX}) - \text{lag3}(\text{CAPX})) / \text{lag3}(\text{CAPX})$
invtgr	Belo and Lin (2011)	$(\text{INVT}/\text{cpi}) / \text{lag1}(\text{INVT}/\text{cpi}) - 1$
invturn	Ou and Penman (1989)	$\text{COGS} / \text{avg2}(\text{INVT})$
issue	Fama and French (2008)	$\log((\text{CSHO} \times \text{AJEX}) / \text{lag1}(\text{CSHO} \times \text{AJEX}))$
issue5	Daniel and Titman (2006)	$\log((\text{CSHO} \times \text{AJEX}) / \text{lag5}(\text{CSHO} \times \text{AJEX}))$
ivolcapm_d	Ang et al. (2006)	The root mean square error of CAPM model using daily returns data over the past 1 month.
ivolcapm_w	Bali and Cakici (2008)	The root mean square error of CAPM using weekly returns data over the past 52 weeks.
ivolff_d	Ang et al. (2006)	The root mean square error of Fama-French 3-Factor model using daily returns data over the past 1 month.
ivolff_w	Bali and Cakici (2008)	The root mean square error of Fama-French 3-Factor model using weekly returns data over the past 52 weeks.
lev	Bhandari (1988)	$\text{LT} / (\text{PRCC.F} \times \text{CSHO})$
ma100	Han et al. (2013)	The end of month PRC / the past 100-day average of daily PRC
ma20	Han et al. (2013)	The end of month PRC / the past 20-day average of daily PRC
ma200	Han et al. (2013)	The end of month PRC / the past 200-day average of daily PRC
ma50	Han et al. (2013)	The end of month PRC / the past 50-day average of daily PRC
maxret	Bali et al. (2011)	The maximum of daily RET over the past 1 month
mom1	Jegadeesh (1990)	$1 + \text{RET}_t$
mom12	Jegadeesh (1990)	$\prod_{i=t-1}^{t-11} (1 + \text{RET}_i)$
mom12_ia	Asness et al. (2000)	mom12 – IndMean(mom12)
mom12_ind	Moskowitz and Grinblatt (1998)	IndMean(mom12)
mom36	DeBondt and Thaler (1985)	$\prod_{i=t}^{t-35} (1 + \text{RET}_i)$
mom36_ia	Asness et al. (2000)	mom36 – IndMean(mom36)
mom6	Jegadeesh and Titman (1993)	$\prod_{i=t-1}^{t-5} (1 + \text{RET}_i)$
mom36	DeBondt and Thaler (1985)	$\prod_{i=t}^{t-59} (1 + \text{RET}_i)$
mom712	Novy-Marx (2012)	$\prod_{i=t-6}^{t-11} (1 + \text{RET}_i)$
nicfo	Ou and Penman (1989)	NI / OANCF
nimr	Ou and Penman (1989)	NI / SALE
noa	Fairfield et al. (2003)	$\text{RECT} + \text{INVT} + \text{PPENT} + \text{ACO} + \text{INTAN} + \text{AO} - \text{AP} - \text{LCO} - \text{LO}$
oimr	Ou and Penman (1989)	$\text{OIBDP} / \text{SALE}$
oita	Ou and Penman (1989)	$\text{EBIT} / \text{avg2}(\text{AT})$
opa	Ball et al. (2015)	$(\text{SALE} - \text{COGS} - (\text{XSGA} - \text{XRD})) / \text{AT}$
orgcap	Eisfeldt and Papanikolaou (2013)	oc/AT^c
orgcap_ia	Eisfeldt and Papanikolaou (2013)	orgcap – IndMean(orgcap)
pchcapx_ia	Lev and Thiagarajan (1993)	$\text{CAPX}/\text{lag1}(\text{CAPX}) - \text{IndMean}(\text{CAPX}/\text{lag1}(\text{CAPX}))$
pchcapxat	Ou and Penman (1989)	$(\text{CAPX} / \text{avg2}(\text{AT})) / \text{lag1}(\text{CAPX} / \text{avg2}(\text{AT})) - 1$
pchcurrat	Ou and Penman (1989)	$\text{currat} / \text{lag1}(\text{currat}) - 1$
pchdebteq	Ou and Penman (1989)	$\text{debteq} / \text{lag1}(\text{debteq}) - 1$
pchdepr	Ou and Penman (1989)	$\text{DP} / \text{lag1}(\text{DP}) - 1$
pchdeprppe	Ou and Penman (1989)	deprppe / $\text{lag1}(\text{deprppe}) - 1$
pchdltt	Ou and Penman (1989)	$\text{DLTT} / \text{lag1}(\text{DLTT}) - 1$

Table B1 (Continued): Annual predictor definition

Variable	Reference	Definition
pchgm_pchsale	Lev and Thiagarajan (1993)	$(\text{SALE} - \text{COGS}) / \text{lag1}(\text{SALE} - \text{COGS}) - \text{SALE} / \text{lag1}(\text{SALE})$
pchgmr	Ou and Penman (1989)	$\text{gmr} / \text{lag1}(\text{gmr}) - 1$
pchinvt	Ou and Penman (1989)	$(\text{INVT} / \text{AT}) / \text{lag1}(\text{INVT} / \text{AT}) - 1$
pchinvtturn	Ou and Penman (1989)	$\text{invturn} / \text{lag1}(\text{invturn}) - 1$
pchnimr	Ou and Penman (1989)	$\text{nimr} / \text{lag1}(\text{nimr}) - 1$
pchoimr	Ou and Penman (1989)	$\text{oimr} / \text{lag1}(\text{oimr}) - 1$
pchoita	Ou and Penman (1989)	$\text{oita} / \text{lag1}(\text{oita}) - 1$
pchpimr	Ou and Penman (1989)	$\text{pimr} / \text{lag1}(\text{pimr}) - 1$
pchppeteq	Ou and Penman (1989)	$\text{ppeteq} / \text{lag1}(\text{ppeteq}) - 1$
pchquick	Ou and Penman (1989)	$\text{quick} / \text{lag1}(\text{quick}) - 1$
pchsale	Ou and Penman (1989)	$\text{SALE} / \text{lag1}(\text{SALE}) - 1$
pchsale_pchinvt	Lev and Thiagarajan (1993)	$\text{SALE} / \text{lag1}(\text{SALE}) - \text{INVT} / \text{lag1}(\text{INVT})$
pchsale_pchrect	Lev and Thiagarajan (1993)	$\text{SALE} / \text{lag1}(\text{SALE}) - \text{RECT} / \text{lag1}(\text{RECT})$
pchsale_pchxsga	Lev and Thiagarajan (1993)	$\text{SALE} / \text{lag1}(\text{SALE}) - \text{XSGA} / \text{lag1}(\text{XSGA})$
pchsaleinv	Ou and Penman (1989)	$\text{saleinv} / \text{lag1}(\text{saleinv}) - 1$
pchsaleta	Ou and Penman (1989)	$\text{saleta} / \text{lag1}(\text{saleta}) - 1$
pchsalewc	Ou and Penman (1989)	$\text{salewcap} / \text{lag1}(\text{salewcap}) - 1$
pchtie	Ou and Penman (1989)	$\text{tie} / \text{lag1}(\text{tie}) - 1$
pchwcap	Ou and Penman (1989)	$(\text{ACT} - \text{LCT}) / \text{lag1}(\text{ACT} - \text{LCT}) - 1$
pchwcapta	Ou and Penman (1989)	$\text{wcapta} / \text{lag1}(\text{wcapta}) - 1$
ptacc	Hafzalla et al. (2011)	$(\Delta \{(\text{ACT} - \text{CHE}) - (\text{LCT} - \text{DLC} - \text{TXP})\} - \text{DP}) / \text{abs}(\text{IB})$
pdelay1	Hou and Moskowitz (2005) ^d	$1 - R_r^2 / R_u^2$
pdelay2	Hou and Moskowitz (2005)	$\sum_{j=1}^4 (j \times d_j) / (b + \sum_{j=1}^4 d_j)$
pdelay3	Hou and Moskowitz (2005)	$\sum_{j=1}^4 (j \times T(d_j)) / (T(b) + \sum_{j=1}^4 T(d_j))$
pimr	Ou and Penman (1989)	PI / SALE
pm	Soliman (2008)	$\text{OIADP} / \text{SALE}$
ppeteq	Ou and Penman (1989)	$\text{PPEGT} / \text{TEQ}$
quick	Ou and Penman (1989)	$(\text{ACT} - \text{INVT}) / \text{LCT}$
rnoa	Soliman (2008)	$\text{OIADP} / \text{avg2}(\text{noa})$
roa	Ou and Penman (1989)	$\text{NI} / \text{avg2}(\text{AT})$
roe	Ou and Penman (1989)	$\text{NI} / \text{avg2}(\text{TEQ})$
roic	Brown and Rowe (2007)	$(\text{EBIT} - \text{NOPI}) / (\text{CEQ} + \text{LT} - \text{CHE})$
salecash	Ou and Penman (1989)	$\text{SALE} / \text{avg2}(\text{CHE})$
saleinv	Ou and Penman (1989)	$\text{SALE} / \text{avg2}(\text{INVT})$
saleppe	Ou and Penman (1989)	$\text{SALE} / \text{avg2}(\text{PPEGT})$
salerec	Ou and Penman (1989)	$\text{SALE} / \text{avg2}(\text{RECT})$
saleta	Ou and Penman (1989)	$\text{SALE} / \text{avg2}(\text{AT})$
salewcap	Ou and Penman (1989)	$\text{SALE} / \text{avg2}(\text{ACT} - \text{LCT})$
season	Keloharju et al. (2016)	The average of $\text{RET}_{t-11}, \text{RET}_{t-23}, \dots, \text{RET}_{t-239}$
size	Banz (1981)	$\text{PRCC.F} \times \text{CSHO}$
size_ia	Asness et al. (2000)	$\text{size} - \text{IndMean}(\text{size})$
sp	Barbee et al. (1996)	$\text{SALE} / (\text{PRCC.F} \times \text{CSHO})$
std_dvol	Chordia et al. (2001)	$\log(\text{lag2}(\text{s.dvol}))$, s.dvol is the standard deviation of $\text{PRC} \times \text{VOL}$ over the past 36 months.
std_turn	Chordia et al. (2001)	$\log(\text{lag2}(\text{s.turn}))$, s.turn is the standard deviation of $\text{VOL} / \text{SHROUT}$ over the past 36 months.
tie	Ou and Penman (1989)	$\text{EBIT} / \text{XINT}$
tangible	Hahn and Lee (2009)	$(\text{CHE} + 0.715 \times \text{RECT} + 0.547 \times \text{INVT} + 0.535 \times \text{PPENT}) / \text{AT}$

Table B1 (Continued): Annual predictor definition

Variable	Reference	Definition
to12	Liu (2006)	The average of daily VOL/SHROUT over the past 12 months.
turn	Chordia et al. (2001)	$\log(\log 2(\text{VOL}/\text{SHROUT}))$
tvol.d	Ang et al. (2006)	The standard deviation of daily RET over the past 1 month
tvol.w	Bali and Cakici (2008)	The standard deviation of weekly RET over the past 52 weeks
wcapta	Ou and Penman (1989)	$(\text{ACT} - \text{LCT}) / \text{AT}$
wh52	George and Hwang (2004)	The end of month PRC / the maximum of daily PRC over the past 12 months
zerotrade	Liu (2006)	$(\text{nzero12} + (1/\text{turn12}) / 11000) \times 21 / \text{ndays12}^e$

Note: The data sources are CRSP and Compustat. The variables with capitalized names are CRSP or Compustat raw variables. The notation $\text{abs}(x)$ denotes the absolute value of x , $\text{lagN}(x)$ denotes x_{t-N} , $\Delta\{x\}$ denotes $x_t - x_{t-N}$, and $\text{avgN}(x)$ denotes the average value of x_t, \dots, x_{t-N+1} . The time series index $\{t, t-1, \dots\}$ indicates monthly frequency for CRSP variables unless explicitly stated otherwise, and t is the portfolio formation time (the end of June). Meanwhile, $\{t, t-1, \dots\}$ of Compustat variables means annual frequency, where t is the latest fiscal year end. Whenever Compustat variables are used, only firms with December fiscal year end are included in the portfolios. $\text{IndMean}(x)$ and $\text{IndSum}(x)$ are the industry mean and sum of x , respectively. We use 2-digit SIC code for the industry classification.

^a For the preferred stock, we use $\text{pref} = \text{PSTKRV}$. We replace PSTKRV with PSTKL if the former is missing. If both PSTKRV and PSTKL are missing, then we use $\text{pref} = \text{PSTK}$.

^b If OANCF is missing, we replace it with $\text{IB} - (\Delta\{(\text{ACT} - \text{CHE}) - (\text{LCT} - \text{DLC} - \text{TXP})\} - \text{DP})$.

^c oc is calculated recursively: $\text{oc}_t = 0.85 \times \text{oc}_{t-1} + \text{XSGA}_t / \text{cpi}_t$, $\text{oc}_0 = 4 \times \text{XSGA}_0 / \text{cpi}_0$.

^d We use the data from the past 52 weeks to estimate the following two regressions:

$$\begin{aligned} r: & \text{RET}_t - \text{Rf}_t = a^r + b^r(\text{Rm}_t - \text{Rf}_t) + \nu_t^r, \\ u: & \text{RET}_t - \text{Rf}_t = a + b(\text{Rm}_t - \text{Rf}_t) + \sum_{k=1}^4 d_k(\text{Rm}_{t-k} - \text{Rf}_{t-k}) + \nu_t, \end{aligned}$$

where Rm and Rf are value-weighted market portfolio returns and one-month Treasury bill rate, respectively. R_r^2 and R_u^2 are the R-squared's of model r and u , respectively. $T(c)$ denotes the ratio between the parameter c and its standard error.

^e nzero12 is the total number of zero trading volume days over the past 12 months, turn12 is the sum of daily VOL/SHROUT over the past 12 months, and ndays12 is the total number of trading days over the past 12 months divided by 12.

B.2 Monthly Predictors

There are 34 monthly predictors defined identically in Table B1: **bas12**, **beta**, **chmom**, **dvol**, **illiq**, **ivolcapm.d**, **ivolcapm.w**, **ivolff.d**, **ivolff.w**, **ma100**, **ma20**, **ma200**, **ma50**, **maxret**, **mom1**, **mom12**, **mom12.ia**, **mom12.ind**, **mom36**, **mom6**, **mom60**, **mom712**, **pdelay1**, **pdelay2**, **pdelay3**, **season**, **std.dvol**, **std.turn**, **to12**, **turn**, **tvol.d**, **tvol.w**, **wh52**, and **zerotrade**.

The additional 11 predictors are summarized below. In each month, we use the earnings information from the most recent announcement date (Compustat Quarterly RDQ). We follow Hou et al. (2015) to assume that the balance sheet data are available with four-month lag after the end of fiscal quarter.

abr (Chan et al., 1996) is the cumulative abnormal returns from RDQ-2 to RDQ+1.

The abnormal return is the stock return minus the equal-weighted market portfolio return. The standardized unexpected earnings **sue** (Chan et al., 1996) is computed as annual change of EPSPXQ divided by its standard deviation computed with the most recent 8 quarterly observations.

dto (Garfinkel and Sokobin, 2006) is calculated as follows

$$\frac{1}{2} \sum_{t=\text{RDQ}-1}^{\text{RDQ}} (\text{turn}_t - \text{turn}_{mt}) - \frac{1}{50} \sum_{t=\text{RDQ}-54}^{\text{RDQ}-5} (\text{turn}_t - \text{turn}_{mt}),$$

where $\text{turn} = \text{VOL}/\text{SHROUT}$ and turn_m is the average of all available turn at time t . To obtain the standardized unexpected volume **suvol** (Garfinkel and Sokobin, 2006), we first run the following regression for each stock with 55 daily observations before RDQ,

$$\text{VOL}_t = a + b_1|\text{RET}|_t^+ + b_2|\text{RET}|_t^- + UV_t,$$

where the plus and minus superscripts indicate the positive and negative parts of the stock return, respectively. We then calculate $\sigma_t(UV)$ as the standard deviation of the residuals over the period $[\text{RDQ}-54, \text{RDQ}-5]$. The variable **suvol** is defined as $\sum_{t=\text{RDQ}-1}^{\text{RDQ}} UV_t$ scaled by $\sigma_t(UV)$.

revmom (Jegadeesh and Livnat, 2006) is annual change in revenue (REVT) divided by its standard deviation calculated with the most recent 8 quarterly observations. **accq** (Collins and Hribar, 2000) is the total accrual normalized by the mean total assets at the end of the two most recent quarters. The accrual is defined as quarterly change in $((\text{ACTQ} - \text{CHEQ}) - (\text{LCTQ} - \text{DLCQ} - \text{TXPQ}))$ minus DPQ. **roaq1**, **roaq2**, and **roaq1** (Balakrishnan et al., 2010) are calculated as IBQ, NIQ, and $(\text{IBQ} - \text{SPIQ})$ scaled by one-quarter lag of ATQ, respectively. **taxmom** (Thomas and Zhang, 2011) is the annual change in tax expense (TXTQ) divided by four-quarter lag of total assets (ATQ). The variable **size** for monthly rebalancing portfolio is defined as $\text{PRC} \times \text{SHROUT}$.

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Supplementary Materials
for
“Do Cross-Sectional Stock Return Predictors Pass
the Test without Data-Snooping Bias?”

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1 Lists of annually rebalanced portfolios with the t -ratios greater than 1.96

Annually rebalanced portfolios with the t -ratios greater than 1.96

Mean (all stocks)			CAPM (all stocks)				
Portfolio	t	α	Portfolio	t	α		
1	grltnoa ^{lh}	4.861	0.732	1	ma100 ^{hl}	5.189	1.214
2	ma100 ^{hl}	4.561	1.092	2	ma200 ^{hl}	5.036	1.313
3	ma200 ^{hl}	4.504	1.220	3	grltnoa ^{lh}	4.935	0.781
4	chceq ^{lh}	4.290	0.989	4	chceq ^{lh}	4.852	1.108
5	illiq ^{hl}	3.817	0.807	5	issue ^{lh}	4.543	1.055
6	issue ^{lh}	3.774	0.888	6	wh52 ^{hl}	4.492	1.273
7	chnco ^{lh}	3.551	0.579	7	tvolf ^{lh}	4.437	1.501
8	agr ^{lh}	3.485	0.803	8	issue5 ^{lh}	4.390	0.832
9	issue5 ^{lh}	3.481	0.707	9	ivolcapm_d ^{lh}	4.214	1.188
10	bm ^{hl}	3.312	0.898	10	tvolf ^{lh}	4.164	1.247
11	mom6 ^{hl}	3.173	0.803	11	ivolff_w ^{lh}	4.022	1.306
12	invtr ^{lh}	3.151	0.527	12	ivolff_d ^{lh}	3.881	1.066
13	sp ^{hl}	3.141	1.045	13	illiq ^{hl}	3.876	0.816
14	pchin ^{lh}	3.112	0.520	14	agr ^{lh}	3.834	0.949
15	chin ^{lh}	3.091	0.632	15	chnco ^{lh}	3.762	0.638
16	cashprod ^{lh}	2.817	0.476	16	ivolcapm_w ^{lh}	3.736	1.221
17	chemp ^{lh}	2.678	0.580	17	invtr ^{lh}	3.603	0.602
18	wh52 ^{hl}	2.676	0.916	18	pchin ^{lh}	3.573	0.596
19	ma50 ^{hl}	2.553	0.662	19	zerotrade ^{hl}	3.493	0.859
20	chmom ^{hl}	2.501	0.564	20	chin ^{lh}	3.459	0.735
21	mom12_ia ^{hl}	2.477	0.591	21	cashprod ^{lh}	3.425	0.571
22	ivolcapm_d ^{lh}	2.434	0.828	22	bm ^{hl}	3.310	0.927
23	std_dvol ^{lh}	2.432	0.388	23	mom6 ^{hl}	3.271	0.806
24	mom12 ^{hl}	2.345	0.713	24	std_dvol ^{lh}	3.235	0.540
25	tvolf ^{lh}	2.281	1.002	25	chemp ^{lh}	3.215	0.732
26	ivolff_w ^{lh}	2.268	0.913	26	maxret ^{lh}	3.143	0.942
27	size_ia ^{lh}	2.221	0.298	27	salerec ^{hl}	3.110	0.520
28	pchppeteq ^{hl}	2.211	0.380	28	bas12 ^{lh}	2.996	1.089
29	acc ^{lh}	2.193	0.431	29	cfodebt ^{hl}	2.941	0.709
30	ivolff_d ^{lh}	2.186	0.720	30	sp ^{hl}	2.882	1.042
31	chfin ^{hl}	2.172	0.382	31	opa ^{hl}	2.863	0.869
32	pchgmr ^{hl}	2.156	0.328	32	ma50 ^{hl}	2.839	0.753
33	saleta ^{hl}	2.150	0.534	33	to12 ^{lh}	2.644	0.684
34	tvolf ^{lh}	2.141	0.815	34	beta ^{lh}	2.639	0.648
35	salerec ^{hl}	2.126	0.378	35	acc ^{lh}	2.596	0.516
36	pchinvt ^{lh}	2.081	0.324	36	pchdebteq ^{hl}	2.576	0.406
37	pchwcap ^{lh}	2.073	0.239	37	mom12_ia ^{hl}	2.566	0.621
38	cfp_ia ^{hl}	2.056	0.441	38	mom12 ^{hl}	2.522	0.787
39	ivolcapm_w ^{lh}	2.001	0.809	39	pchwcap ^{lh}	2.510	0.297
40	chwc ^{lh}	1.972	0.375	40	cfp ^{hl}	2.453	0.610
41	pctacc ^{lh}	1.964	0.292	41	chwc ^{lh}	2.393	0.466
				42	pm ^{hl}	2.380	0.715
				43	chmom ^{hl}	2.363	0.556
				44	turn ^{lh}	2.321	0.595
				45	std_turn ^{lh}	2.315	0.548
				46	pctacc ^{lh}	2.286	0.346
				47	dvol ^{lh}	2.242	0.432
				48	pchppeteq ^{hl}	2.220	0.394
				49	ppeteq ^{hl}	2.206	0.591
				50	pchinvt ^{lh}	2.183	0.338
				51	invest_LWZ ^{lh}	2.171	0.666
				52	invest_AG ^{lh}	2.125	0.410
				53	chemp_ia ^{lh}	2.086	0.443
				54	pchgmr ^{hl}	2.070	0.324
				55	pimr ^{hl}	2.048	0.614
				56	oimr ^{hl}	2.032	0.604

Annually rebalanced portfolios with the t -ratios greater than 1.96

3-Factor (all stocks)			4-Factor (all stocks)				
Portfolio	t	α	Portfolio	t	α		
1	ma200 ^{hl}	5.786	1.529	1	tvolf_w ^{lh}	4.214	1.162
2	wh52 ^{hl}	5.576	1.389	2	issue ^{lh}	4.032	0.754
3	ma100 ^{hl}	5.511	1.415	3	ivolf_w ^{lh}	3.894	1.061
4	ivolcapm_d ^{lh}	4.936	1.152	4	illiq ^{hl}	3.863	0.539
5	tvolf_w ^{lh}	4.849	1.335	5	ivolcapm_d ^{lh}	3.832	0.976
6	ivolf_d ^{lh}	4.732	1.026	6	ivolcapm_w ^{lh}	3.827	1.013
7	ivolf_w ^{lh}	4.564	1.221	7	tvolf_d ^{lh}	3.467	0.962
8	illiq ^{hl}	4.523	0.623	8	ivolf_d ^{lh}	3.402	0.834
9	tvolf_d ^{lh}	4.319	1.158	9	issue5 ^{lh}	3.327	0.707
10	issue ^{lh}	4.314	0.818	10	chceq ^{lh}	3.132	0.700
11	mom12_ia ^{hl}	4.278	0.904	11	grltnoa ^{lh}	3.108	0.511
12	ma50 ^{hl}	4.215	1.071	12	chfn ^{hl}	2.967	0.545
13	ivolcapm_w ^{lh}	4.202	1.128	13	maxret ^{lh}	2.751	0.683
14	mom12 ^{hl}	4.141	1.089	14	cfodebt ^{hl}	2.745	0.596
15	grltnoa ^{lh}	4.073	0.595	15	opa ^{hl}	2.607	0.782
16	issue5 ^{lh}	4.016	0.810	16	ma100 ^{hl}	2.466	0.741
17	chceq ^{lh}	3.903	0.779	17	wh52 ^{hl}	2.327	0.641
18	bas12 ^{lh}	3.723	1.035	18	chnco ^{lh}	2.325	0.392
19	mom6 ^{hl}	3.406	0.854	19	ma200 ^{hl}	2.325	0.682
20	mom1 ^{hl}	3.229	0.846	20	std_dvol ^{lh}	2.260	0.245
21	chfn ^{hl}	3.140	0.530	21	bas12 ^{lh}	2.222	0.689
22	opa ^{hl}	3.100	0.925	22	pm ^{hl}	2.208	0.492
23	agr ^{lh}	2.967	0.524	23	salerec ^{hl}	2.198	0.379
24	maxret ^{lh}	2.862	0.739	24	pchdeprppe ^{hl}	2.182	0.393
25	cfodebt ^{hl}	2.839	0.612	25	acc ^{lh}	2.125	0.464
26	chnco ^{lh}	2.755	0.451	26	roic ^{hl}	2.124	0.560
27	std_dvol ^{lh}	2.701	0.294	27	agr ^{lh}	2.098	0.378
28	acc ^{lh}	2.618	0.514	28	ma50 ^{hl}	2.038	0.545
29	pchgmr ^{hl}	2.588	0.391				
30	chpm ^{hl}	2.586	0.572				
31	ma20 ^{hl}	2.566	0.571				
32	salerec ^{hl}	2.557	0.449				
33	chinv ^{lh}	2.526	0.497				
34	invtr ^{lh}	2.456	0.406				
35	pm ^{hl}	2.454	0.569				
36	pchinv ^{lh}	2.429	0.402				
37	pimr ^{hl}	2.306	0.558				
38	zerotrade ^{hl}	2.259	0.450				
39	chemp ^{lh}	2.247	0.388				
40	gpa_ia ^{hl}	2.238	0.468				
41	chwc ^{lh}	2.215	0.423				
42	mom60 ^{hl}	2.171	0.441				
43	pchdeprppe ^{hl}	2.102	0.360				
44	pchdlt ^{lh}	1.999	0.318				

Annually rebalanced portfolios with the t -ratios greater than 1.96

5-Factor (all stocks)			Q-Factor (all stocks)				
Portfolio	t	α	Portfolio	t	α		
1	ma50 ^{hl}	5.017	1.259	1	illiq ^{hl}	3.437	0.569
2	ma200 ^{hl}	4.646	1.420	2	cashprod ^{lh}	3.397	0.490
3	mom1 ^{hl}	4.505	1.140	3	cfp_ia ^{hl}	3.144	0.760
4	ma100 ^{hl}	4.415	1.314	4	bm_ia ^{hl}	2.704	0.602
5	illiq ^{hl}	4.359	0.654	5	ma200 ^{hl}	2.531	0.844
6	noa ^{lh}	3.961	0.757	6	pchdepr ^{hl}	2.440	0.577
7	chfn ^{hl}	3.740	0.654	7	noa ^{lh}	2.424	0.660
8	mom12_ia ^{hl}	3.690	0.864	8	ma50 ^{hl}	2.356	0.719
9	wh52 ^{hl}	3.545	0.942	9	acc ^{lh}	2.338	0.520
10	ma20 ^{hl}	3.526	0.840	10	gpa ^{lh}	2.333	0.524
11	mom12 ^{hl}	3.391	0.912	11	invest_LWZ ^{hl}	2.323	0.692
12	quick ^{hl}	3.390	0.557	12	mom36 ^{hl}	2.321	0.599
13	lev ^{lh}	3.239	0.531	13	pchdeprppe ^{hl}	2.264	0.461
14	invest_LWZ ^{hl}	3.140	0.612	14	chwc ^{lh}	2.261	0.498
15	chpm ^{hl}	2.917	0.761	15	chfn ^{hl}	2.222	0.464
16	cfp_ia ^{hl}	2.878	0.593	16	mom12_ia ^{hl}	2.145	0.610
17	cashprod ^{lh}	2.843	0.376	17	ma100 ^{hl}	2.112	0.697
18	cash ^{hl}	2.815	0.596	18	tvoll_w ^{lh}	2.072	0.668
19	tangible ^{hl}	2.814	0.584	19	mom1 ^{hl}	1.966	0.649
20	tvoll_w ^{lh}	2.780	0.617				
21	salecash ^{lh}	2.777	0.559				
22	mom6 ^{hl}	2.742	0.805				
23	debteq ^{lh}	2.704	0.467				
24	ivolcapm_d ^{lh}	2.694	0.534				
25	acc ^{lh}	2.579	0.509				
26	currat ^{hl}	2.493	0.403				
27	size ^{lh}	2.449	0.488				
28	ivolff_w ^{lh}	2.350	0.551				
29	gpa ^{lh}	2.330	0.386				
30	chceq ^{lh}	2.293	0.431				
31	pchdeprppe ^{hl}	2.271	0.396				
32	issue5 ^{lh}	2.220	0.373				
33	std_dvol ^{lh}	2.216	0.242				
34	pchsale ^{hl}	2.198	0.417				
35	pchdepr ^{hl}	2.192	0.392				
36	chwc ^{lh}	2.183	0.423				
37	deprppe ^{hl}	2.149	0.468				
38	mom36 ^{hl}	2.147	0.460				
39	size_ia ^{lh}	2.120	0.224				
40	orgcap ^{hl}	2.094	0.434				
41	tvoll_d ^{lh}	2.039	0.507				
42	bm_ia ^{hl}	2.033	0.384				
43	salerec ^{hl}	1.983	0.338				
44	pchwcapta ^{lh}	1.974	0.184				
45	ivolcapm_w ^{lh}	1.965	0.445				
46	issue ^{lh}	1.963	0.299				
47	ivolff_d ^{lh}	1.962	0.389				

Annually rebalanced portfolios with the t -ratios greater than 1.96

Mean (all-but-tiny stocks)			CAPM (all-but-tiny stocks)				
Portfolio	t	α	Portfolio	t	α		
1	issue5 ^{lh}	3.647	0.713	1	issue5 ^{lh}	4.440	0.844
2	issue ^{lh}	3.614	0.831	2	wh52 ^{hl}	4.367	0.834
3	chinv ^{lh}	3.523	0.544	3	cfp ^{hl}	4.079	0.889
4	chnco ^{lh}	3.450	0.542	4	chceq ^{lh}	3.999	0.945
5	grltnoa ^{lh}	3.297	0.524	5	issue ^{lh}	3.979	0.953
6	chceq ^{lh}	3.152	0.753	6	chinv ^{lh}	3.955	0.625
7	cfp ^{hl}	3.091	0.701	7	chnco ^{lh}	3.800	0.611
8	pchinv ^{lh}	3.027	0.489	8	pchinv ^{lh}	3.518	0.570
9	invtgr ^{lh}	3.025	0.489	9	invtgr ^{lh}	3.516	0.569
10	mom6 ^{hl}	2.843	0.662	10	grltnoa ^{lh}	3.509	0.587
11	agr ^{lh}	2.739	0.634	11	tvolf ^{lh}	3.386	0.960
12	chwc ^{lh}	2.678	0.427	12	beta ^{lh}	3.359	0.856
13	dvol ^{lh}	2.546	0.338	13	agr ^{lh}	3.336	0.814
14	ma100 ^{hl}	2.532	0.622	14	tvolf ^{lh}	3.201	0.790
15	ma200 ^{hl}	2.520	0.674	15	chwc ^{lh}	3.093	0.502
16	chmom ^{hl}	2.495	0.538	16	ivolcapm _w ^{lh}	3.065	0.778
17	sp ^{hl}	2.417	0.711	17	std_dvol ^{lh}	3.040	0.427
18	size.ia ^{lh}	2.396	0.313	18	dvol ^{lh}	2.978	0.404
19	std_dvol ^{lh}	2.338	0.326	19	bas12 ^{lh}	2.969	0.929
20	bm ^{hl}	2.332	0.568	20	cashprod ^{lh}	2.833	0.508
21	pchppeteq ^{hl}	2.319	0.369	21	ma100 ^{hl}	2.734	0.663
22	illiq ^{hl}	2.291	0.298	22	mom6 ^{hl}	2.660	0.605
23	pchwcap ^{lh}	2.284	0.284	23	salerec ^{hl}	2.642	0.364
24	cashprod ^{lh}	2.244	0.409	24	pchwcap ^{lh}	2.590	0.332
25	mom12.ia ^{hl}	2.219	0.454	25	ivolf _w ^{lh}	2.580	0.652
26	wh52 ^{hl}	2.174	0.522	26	chemp ^{lh}	2.552	0.572
27	pchdebteq ^{hl}	2.134	0.353	27	bm ^{hl}	2.546	0.659
28	pchsalewc ^{hl}	2.065	0.224	28	ep ^{hl}	2.542	0.614
29	chemp ^{lh}	1.983	0.427	29	pchdebteq ^{hl}	2.524	0.439
				30	ma200 ^{hl}	2.524	0.684
				31	chmom ^{hl}	2.454	0.554
				32	turn ^{lh}	2.394	0.616
				33	zerotrade ^{hl}	2.374	0.611
				34	sp ^{hl}	2.309	0.753
				35	ivolf _d ^{lh}	2.286	0.543
				36	ppeteq ^{hl}	2.276	0.595
				37	pchppeteq ^{hl}	2.257	0.384
				38	acc ^{lh}	2.257	0.365
				39	maxret ^{lh}	2.235	0.593
				40	illiq ^{hl}	2.157	0.279
				41	chemp_ia ^{lh}	2.156	0.416
				42	ivolcapm _d ^{lh}	2.156	0.508
				43	invest_AG ^{lh}	2.115	0.392
				44	to12 ^{lh}	2.111	0.566
				45	pdelay1 ^{hl}	2.108	0.332
				46	invest_LWZ ^{lh}	2.067	0.647
				47	opa ^{hl}	2.043	0.518
				48	cfodebt ^{hl}	1.994	0.385
				49	std_turn ^{lh}	1.986	0.458

Annually rebalanced portfolios with the t -ratios greater than 1.96

3-Factor (all-but-tiny stocks)			4-Factor (all-but-tiny stocks)				
Portfolio	t	α	Portfolio	t	α		
1	wh52 ^{hl}	4.811	0.915	1	issue ^{lh}	3.824	0.662
2	issue ^{lh}	4.128	0.731	2	issue5 ^{lh}	3.091	0.599
3	issue5 ^{lh}	3.888	0.750	3	gmr ^{hl}	2.611	0.424
4	ma200 ^{hl}	3.861	0.988	4	chnco ^{lh}	2.427	0.384
5	mom12_ia ^{hl}	3.852	0.702	5	grltnoa ^{lh}	2.395	0.395
6	ma100 ^{hl}	3.509	0.903	6	chceq ^{lh}	2.213	0.382
7	ma50 ^{hl}	3.277	0.764	7	tvolf_w ^{lh}	2.192	0.491
8	mom12 ^{hl}	3.270	0.725	8	chfin ^{hl}	2.166	0.384
9	chnco ^{lh}	3.112	0.474	9	cfodebt ^{hl}	2.165	0.446
10	tvolf_w ^{lh}	3.085	0.672	10	ivolcapm_w ^{lh}	2.112	0.433
11	chceq ^{lh}	2.984	0.524	11	cfp ^{hl}	2.098	0.339
12	grltnoa ^{lh}	2.936	0.452	12	agr ^{lh}	2.045	0.324
13	chinv ^{lh}	2.934	0.436				
14	mom1 ^{hl}	2.831	0.699				
15	ivolcapm_w ^{lh}	2.745	0.565				
16	tvolf_d ^{lh}	2.696	0.539				
17	beta ^{lh}	2.686	0.560				
18	opa ^{hl}	2.674	0.616				
19	chwc ^{lh}	2.653	0.455				
20	mom6 ^{hl}	2.597	0.620				
21	cfp ^{hl}	2.574	0.445				
22	gmr ^{hl}	2.571	0.437				
23	ma20 ^{hl}	2.565	0.637				
24	bas12 ^{lh}	2.472	0.638				
25	agr ^{lh}	2.422	0.396				
26	cfodebt ^{hl}	2.282	0.454				
27	chpm ^{hl}	2.266	0.446				
28	ato ^{hl}	2.250	0.381				
29	pchinv ^{lh}	2.234	0.355				
30	invtgr ^{lh}	2.231	0.354				
31	ivolff_w ^{lh}	2.218	0.450				
32	pchsalewc ^{hl}	2.176	0.242				
33	chfin ^{hl}	2.167	0.340				
34	pchoita ^{hl}	2.141	0.392				
35	gpa ^{hl}	2.067	0.403				
36	pchdebteq ^{hl}	2.064	0.312				
37	acc ^{lh}	2.052	0.337				
38	salerec ^{hl}	1.985	0.297				

Annually rebalanced portfolios with the t -ratios greater than 1.96

5-Factor (all-but-tiny stocks)			Q-Factor (all-but-tiny stocks)				
Portfolio	t	α	Portfolio	t	α		
1	noa ^{lh}	4.916	0.692	1	cashprod ^{lh}	3.012	0.492
2	ma50 ^{hl}	4.700	1.091	2	bm_ia ^{hl}	2.907	0.622
3	mom1 ^{hl}	4.458	1.063	3	pchdepr ^{hl}	2.758	0.624
4	quick ^{hl}	4.316	0.695	4	invest_LWZ ^{hl}	2.751	0.825
5	salecash ^{lh}	4.219	0.714	5	pchsale ^{hl}	2.636	0.564
6	mom12_ia ^{hl}	4.017	0.785	6	cfp_ia ^{hl}	2.635	0.540
7	ma20 ^{hl}	3.863	0.995	7	quick ^{hl}	2.438	0.587
8	pchsale ^{hl}	3.817	0.600	8	salecash ^{lh}	2.365	0.691
9	debteq ^{lh}	3.708	0.574	9	em ^{lh}	2.364	0.649
10	ma200 ^{hl}	3.697	1.038	10	noa ^{lh}	2.225	0.520
11	invest_LWZ ^{hl}	3.488	0.685	11	mom12_ia ^{hl}	2.174	0.541
12	lev ^{lh}	3.458	0.550	12	rnoa ^{lh}	2.137	0.452
13	tangible ^{hl}	3.442	0.656	13	chemp ^{hl}	2.066	0.357
14	cash ^{hl}	3.343	0.565	14	oita ^{lh}	2.057	0.577
15	ma100 ^{hl}	3.195	0.990	15	pchwcapta ^{lh}	2.056	0.230
16	pchdepr ^{hl}	3.186	0.520	16	gpa ^{lh}	2.053	0.443
17	mom12 ^{hl}	3.074	0.688	17	debteq ^{lh}	2.004	0.478
18	chpm ^{hl}	2.977	0.669	18	mom1 ^{hl}	1.986	0.636
19	wh52 ^{hl}	2.931	0.574	19	saleta ^{lh}	1.981	0.399
20	currat ^{hl}	2.920	0.454				
21	wcapta ^{hl}	2.816	0.467				
22	chfin ^{hl}	2.786	0.445				
23	cashprod ^{lh}	2.627	0.349				
24	oimr ^{lh}	2.511	0.465				
25	bm_ia ^{hl}	2.429	0.468				
26	mve ^{lh}	2.393	0.293				
27	pm ^{lh}	2.364	0.486				
28	size_ia ^{lh}	2.364	0.234				
29	roe ^{lh}	2.284	0.468				
30	pchsale_pchxsga ^{hl}	2.250	0.413				
31	oita ^{lh}	2.245	0.475				
32	pchwcapta ^{lh}	2.174	0.213				
33	ppeteq ^{lh}	2.171	0.379				
34	nimr ^{lh}	2.116	0.387				
35	roa ^{lh}	2.067	0.409				
36	em ^{lh}	2.012	0.484				
37	issue5 ^{lh}	2.010	0.306				
38	sp ^{lh}	2.000	0.370				
39	pchsaleinv ^{hl}	1.995	0.364				

2 Lists of monthly rebalanced portfolios with the t -ratios greater than 1.96

Monthly rebalanced portfolios with the t -ratios greater than 1.96

Mean (all stocks)			CAPM (all stocks)				
Portfolio	t	α	Portfolio	t	α		
1	abr ^{hl}	6.747	1.187	1	abr ^{hl}	7.053	1.215
2	mom712 ^{hl}	5.237	1.615	2	tvolf_d ^{lh}	5.621	2.146
3	ma20 ^{lh}	4.664	0.993	3	mom12 ^{hl}	5.553	2.159
4	mom12 ^{hl}	4.432	1.915	4	ivolf_d ^{lh}	5.457	1.941
5	mom12_ia ^{hl}	3.632	1.290	5	tvolf_w ^{lh}	5.317	2.078
6	mom6 ^{hl}	3.553	1.361	6	mom712 ^{hl}	5.238	1.643
7	ivolf_d ^{lh}	3.527	1.469	7	ivolcapm_d ^{lh}	5.100	1.889
8	ivolcapm_d ^{lh}	3.208	1.404	8	maxret ^{lh}	5.028	1.554
9	sue ^{hl}	3.161	0.441	9	ivolf_w ^{lh}	4.820	1.868
10	illiq ^{hl}	3.101	0.713	10	ivolcapm_w ^{lh}	4.645	1.792
11	tvolf_d ^{lh}	2.992	1.446	11	mom6 ^{hl}	4.603	1.611
12	roaq1 ^{hl}	2.867	0.816	12	mom12_ia ^{hl}	4.360	1.424
13	roaq2 ^{hl}	2.814	0.790	13	roaq3 ^{hl}	4.302	1.265
14	roaq3 ^{hl}	2.794	0.928	14	roaq2 ^{hl}	4.074	1.055
15	tvolf_w ^{lh}	2.680	1.357	15	roaq1 ^{hl}	4.054	1.072
16	ivolf_w ^{lh}	2.648	1.287	16	sue ^{hl}	3.913	0.539
17	taxmom ^{hl}	2.623	0.423	17	wh52 ^{hl}	3.801	1.433
18	maxret ^{lh}	2.594	1.006	18	ma20 ^{lh}	3.638	0.771
19	ivolcapm_w ^{lh}	2.516	1.217	19	bas12 ^{lh}	3.562	1.565
20	accq ^{lh}	2.322	0.356	20	zerotrade ^{hl}	3.436	0.955
21	season ^{hl}	2.278	0.475	21	illiq ^{hl}	3.361	0.804
22	size ^{lh}	2.269	0.748	22	std_dvol ^{lh}	3.191	0.628
23	std_dvol ^{lh}	2.129	0.391	23	revmom ^{hl}	3.077	0.437
24	revmom ^{hl}	2.065	0.299	24	taxmom ^{hl}	2.480	0.391
				25	accq ^{lh}	2.436	0.371
				26	size ^{lh}	2.336	0.774
				27	ma200 ^{hl}	2.330	0.906
				28	to12 ^{lh}	2.282	0.669
				29	beta ^{lh}	2.214	0.724
				30	dvol ^{lh}	2.034	0.435
				31	turn ^{lh}	2.031	0.587
				32	std_turn ^{lh}	2.029	0.572

Monthly rebalanced portfolios with the t -ratios greater than 1.96

3-Factor (all stocks)			4-Factor (all stocks)				
Portfolio	t	α	Portfolio	t	α		
1	ivolff_d^{lh}	7.219	1.962	1	abr^{hl}	6.124	1.071
2	abr^{hl}	7.183	1.289	2	ivolff_d^{lh}	4.995	1.547
3	ivolcapm_d^{lh}	6.695	1.913	3	tvolf_d^{lh}	4.978	1.710
4	mom712^{hl}	6.625	1.879	4	tvolf_w^{lh}	4.768	1.725
5	tvolf_d^{lh}	6.523	2.102	5	ivolff_w^{lh}	4.604	1.563
6	mom12^{hl}	6.456	2.381	6	ivolcapm_d^{lh}	4.573	1.460
7	ivolff_w^{lh}	6.399	1.933	7	ivolcapm_w^{lh}	4.556	1.521
8	ivolcapm_w^{lh}	6.276	1.850	8	maxret^{lh}	4.490	1.231
9	tvolf_w^{lh}	6.205	2.033	9	ma20^{lh}	4.386	1.013
10	mom12_ia^{hl}	6.020	1.711	10	mom12^{hl}	4.137	0.880
11	maxret^{lh}	5.990	1.531	11	roaq2^{hl}	3.953	0.950
12	roaq2^{hl}	5.076	1.202	12	roaq3^{hl}	3.812	1.051
13	roaq1^{hl}	4.947	1.198	13	roaq1^{hl}	3.720	0.934
14	mom6^{hl}	4.940	1.700	14	mom712^{hl}	3.672	0.940
15	roaq3^{hl}	4.923	1.328	15	illiq^{hl}	3.518	0.532
16	wh52^{hl}	4.726	1.569	16	mom12_ia^{hl}	3.450	0.731
17	bas12^{lh}	4.455	1.616	17	size^{lh}	3.185	0.881
18	taxmom^{hl}	3.864	0.557	18	bas12^{lh}	2.790	1.132
19	illiq^{hl}	3.689	0.532	19	accq^{lh}	2.628	0.381
20	revmom^{hl}	3.403	0.429	20	taxmom^{hl}	2.502	0.344
21	sue^{hl}	3.396	0.512	21	zerotrade^{hl}	2.499	0.521
22	ma20^{lh}	3.268	0.722	22	std_dvol^{lh}	2.367	0.319
23	season^{hl}	2.804	0.552	23	revmom^{hl}	2.225	0.302
24	zerotrade^{hl}	2.802	0.599	24	sue^{hl}	2.188	0.329
25	ma200^{hl}	2.767	1.031	25	chmom^{lh}	2.039	0.526
26	std_dvol^{lh}	2.699	0.360				
27	accq^{lh}	2.680	0.414				
28	mom12_ind^{hl}	2.325	0.714				
29	size^{lh}	2.150	0.514				

5-Factor (all stocks)			Q-Factor (all stocks)				
Portfolio	t	α	Portfolio	t	α		
1	abr^{hl}	7.005	1.342	1	abr^{hl}	5.225	1.103
2	mom712^{hl}	5.210	1.625	2	ma20^{lh}	4.155	1.182
3	mom12_ia^{hl}	4.258	1.495	3	tvolf_w^{lh}	2.916	0.939
4	ivolff_w^{lh}	3.943	0.991	4	ivolff_d^{lh}	2.815	0.939
5	tvolf_w^{lh}	3.942	1.026	5	mom712^{hl}	2.755	0.941
6	ivolff_d^{lh}	3.834	1.118	6	illiq^{hl}	2.707	0.464
7	tvolf_d^{lh}	3.757	1.094	7	size^{lh}	2.697	1.035
8	illiq^{hl}	3.744	0.551	8	ivolcapm_w^{lh}	2.670	0.832
9	ivolcapm_w^{lh}	3.648	0.922	9	tvolf_d^{lh}	2.654	0.901
10	mom12^{hl}	3.492	1.750	10	ivolff_w^{lh}	2.559	0.815
11	ma20^{lh}	3.399	0.866	11	accq^{lh}	2.515	0.436
12	taxmom^{hl}	3.259	0.507	12	season^{hl}	2.508	0.546
13	season^{hl}	3.244	0.643	13	ivolcapm_d^{lh}	2.129	0.745
14	ivolcapm_d^{lh}	3.224	1.009	14	maxret^{lh}	2.051	0.588
15	size^{lh}	3.086	0.911				
16	maxret^{lh}	3.025	0.719				
17	accq^{lh}	2.974	0.525				
18	mom6^{hl}	2.842	1.314				
19	roaq2^{hl}	2.458	0.467				
20	roaq1^{hl}	2.402	0.472				
21	pdelay3^{lh}	2.366	0.244				
22	revmom^{hl}	2.359	0.298				
23	roaq3^{hl}	2.320	0.515				
24	std_dvol^{lh}	2.138	0.288				
25	sue^{hl}	2.116	0.312				
26	pdelay2^{lh}	2.085	0.211				

Monthly rebalanced portfolios with the t -ratios greater than 1.96

Mean (all-but-tiny stocks)			CAPM (all-but-tiny stocks)				
Portfolio	t	α	Portfolio	t	α		
1	abr ^{hl}	4.690	0.764	1	abr ^{hl}	5.038	0.788
2	ma20 ^{lh}	4.663	0.860	2	tvold ^{lh}	4.437	1.458
3	mom712 ^{hl}	4.136	1.241	3	ivolcapm_d ^{lh}	4.266	1.246
4	mom12 ^{hl}	3.584	1.259	4	mom12 ^{hl}	3.965	1.327
5	sue ^{hl}	2.997	0.434	5	maxret ^{lh}	3.943	1.062
6	illiq ^{hl}	2.996	0.453	6	ivolf_d ^{lh}	3.940	1.145
7	mom12_ia ^{hl}	2.950	0.928	7	ma20 ^{lh}	3.785	0.696
8	mom6 ^{hl}	2.631	0.842	8	sue ^{hl}	3.682	0.528
9	accq ^{lh}	2.410	0.339	9	tvol_w ^{lh}	3.676	1.198
10	roaq1 ^{hl}	2.311	0.623	10	mom712 ^{hl}	3.624	1.146
11	season ^{hl}	2.242	0.420	11	ivolcapm_w ^{lh}	3.427	1.044
12	taxmom ^{hl}	2.189	0.327	12	roaq3 ^{hl}	3.269	0.911
13	chmom ^{lh}	2.165	0.547	13	roaq1 ^{hl}	3.238	0.845
14	std_dvol ^{lh}	2.140	0.352	14	bas12 ^{lh}	3.232	1.157
15	roaq2 ^{hl}	2.130	0.548	15	ivolf_w ^{lh}	3.160	0.939
16	roaq3 ^{hl}	2.088	0.627	16	mom6 ^{hl}	3.120	0.950
17	dvol ^{lh}	2.033	0.301	17	std_dvol ^{lh}	3.112	0.517
				18	roaq2 ^{hl}	3.020	0.755
				19	wh52 ^{hl}	2.956	0.903
				20	revmom ^{hl}	2.937	0.427
				21	mom12_ia ^{hl}	2.933	0.919
				22	beta ^{lh}	2.852	0.860
				23	illiq ^{hl}	2.817	0.453
				24	dvol ^{lh}	2.772	0.420
				25	accq ^{lh}	2.412	0.340
				26	zerotrade ^{hl}	2.110	0.642
				27	suvo1 ^{lh}	2.010	0.280

3-Factor (all-but-tiny stocks)			4-Factor (all-but-tiny stocks)				
Portfolio	t	α	Portfolio	t	α		
1	abr ^{hl}	5.478	0.870	1	abr ^{hl}	4.170	0.638
2	mom712 ^{hl}	5.240	1.403	2	ma20 ^{lh}	4.165	0.930
3	mom12 ^{hl}	5.110	1.560	3	tvold ^{lh}	3.492	1.002
4	ivolcapm_d ^{lh}	4.804	1.134	4	ivolcapm_d ^{lh}	3.253	0.804
5	ivolf_d ^{lh}	4.675	1.022	5	ivolf_d ^{lh}	3.157	0.730
6	tvold ^{lh}	4.665	1.264	6	maxret ^{lh}	2.821	0.696
7	mom12_ia ^{hl}	4.551	1.179	7	roaq1 ^{hl}	2.807	0.712
8	roaq1 ^{hl}	4.045	0.963	8	chmom ^{lh}	2.741	0.734
9	maxret ^{lh}	3.919	0.901	9	roaq3 ^{hl}	2.719	0.729
10	roaq2 ^{hl}	3.895	0.888	10	roaq2 ^{hl}	2.653	0.660
11	roaq3 ^{hl}	3.840	1.004	11	tvol_w ^{lh}	2.481	0.706
12	tvol_w ^{lh}	3.800	0.993	12	mom712 ^{hl}	2.418	0.587
13	ivolcapm_w ^{lh}	3.423	0.905	13	ivolcapm_w ^{lh}	2.400	0.679
14	taxmom ^{hl}	3.365	0.445	14	ma200 ^{lh}	2.290	0.541
15	ma20 ^{lh}	3.347	0.665	15	accq ^{lh}	2.179	0.322
16	mom6 ^{hl}	3.323	1.017	16	ivolf_w ^{lh}	2.168	0.580
17	wh52 ^{hl}	3.277	0.940	17	season ^{hl}	2.151	0.367
18	revmom ^{hl}	3.264	0.426	18	revmom ^{hl}	2.027	0.287
19	ivolf_w ^{lh}	3.257	0.814	19	sue ^{hl}	1.962	0.303
20	sue ^{hl}	3.146	0.488				
21	bas12 ^{lh}	3.093	0.934				
22	season ^{hl}	2.785	0.494				
23	accq ^{lh}	2.430	0.350				
24	beta ^{lh}	2.402	0.659				
25	illiq ^{hl}	2.376	0.232				
26	ma200 ^{hl}	2.131	0.684				
27	std_dvol ^{lh}	2.008	0.195				

Monthly rebalanced portfolios with the t -ratios greater than 1.96

5-Factor (all-but-tiny stocks)			Q-Factor (all-but-tiny stocks)		
Portfolio	t	α	Portfolio	t	α
1 abr ^{hl}	5.091	0.903	1 ma20 ^{lh}	4.248	1.079
2 mom712 ^{hl}	4.419	1.282	2 abr ^{hl}	2.882	0.597
3 ma20 ^{lh}	3.514	0.774	3 season ^{hl}	2.825	0.514
4 mom12_ia ^{hl}	3.349	1.092	4 accq ^{lh}	2.410	0.430
5 season ^{hl}	3.152	0.547			
6 taxmom ^{hl}	2.989	0.432			
7 accq ^{lh}	2.921	0.470			
8 mom12 ^{hl}	2.691	1.180			
9 illiq ^{hl}	2.686	0.281			
10 std_turn ^{hl}	2.390	0.427			
11 turn ^{hl}	2.363	0.513			
12 tvold ^{lh}	2.283	0.479			
13 revmom ^{hl}	2.236	0.300			
14 ivolcapm.d ^{lh}	2.045	0.418			
15 mom6 ^{hl}	2.022	0.840			

3 Selective inference with multiple families

Selective inference (Mean)

	Studentized		Non-studentized	
	CV	Significant portfolios	CV	Significant portfolios
All stocks.				
Value	2.618	bm ^{hl} (3.312), sp ^{hl} (3.141).	0.713	sp ^{hl} (1.045), bm ^{hl} (0.898).
Momentum	2.104	ma100 ^{hl} (4.561), ma200 ^{hl} (4.504), mom6 ^{hl} (3.173), wh52 ^{hl} (2.676), ma50 ^{hl} (2.553), mom12_ia ^{hl} (2.477), mom12 ^{hl} (2.345).	0.626	ma200 ^{hl} (1.220), ma100 ^{hl} (1.092), wh52 ^{hl} (0.916), mom6 ^{hl} (0.803), mom12 ^{hl} (0.713), ma50 ^{hl} (0.662).
Volatility	2.246	ivolcapm.d ^{lh} (2.434), tvol.w ^{lh} (2.281), ivolff.w ^{lh} (2.268).	0.617	tvol.w ^{lh} (1.002), ivolff.w ^{lh} (0.913), ivolcapm.d ^{lh} (0.828), tvol.d ^{lh} (0.815), ivolcapm.w ^{lh} (0.809), ivolff.d ^{lh} (0.720).
Growth	2.440	grltnoa ^{lh} (4.861), issue ^{lh} (3.774), agr ^{lh} (3.485), issue5 ^{lh} (3.481).	0.636	issue ^{lh} (0.888), agr ^{lh} (0.803), grltnoa ^{lh} (0.732), issue5 ^{lh} (0.707).
Profitability		#		
Trading	2.619	illiq ^{hl} (3.817).	0.707	illiq ^{hl} (0.807).
Others	3.363	chceq ^{lh} (4.290), chnco ^{lh} (3.551).	0.920	chceq ^{lh} (4.290).
All-but-tiny stocks.				
Value	2.806	cfp ^{hl} (3.091)	0.625	sp ^{hl} (0.711), cfp ^{hl} (0.701).
Momentum	2.57	mom6 ^{hl} (2.843)	0.639	ma200 ^{hl} (0.674), mom6 ^{hl} (0.662).
Volatility		#		
Growth	2.528	issue5 ^{lh} (3.647), issue ^{lh} (3.614), grltnoa ^{lh} (3.297), agr ^{lh} (2.739).	0.668	issue ^{lh} (0.831), issue5 ^{lh} (0.713).
Profitability		#		
Trading	2.602	–	0.717	–
Others	3.527	–	0.869	–

Selective inference (CAPM)

	Studentized		Non-studentized	
	CV	Significant portfolios	CV	Significant portfolios
All stocks.				
Value	2.544	bm ^{hl} (3.310), sp ^{hl} (2.882).	0.630	sp ^{hl} (1.042), bm ^{hl} (0.927).
Momentum	2.044	ma100 ^{hl} (5.189), ma200 ^{hl} (5.036), wh52 ^{hl} (4.492), mom6 ^{hl} (3.271), ma50 ^{hl} (2.839), mom12 ^{ia} (2.566), mom12 ^{hl} (2.522)	0.647	ma200 ^{hl} (1.313), wh52 ^{hl} (1.273), ma100 ^{hl} (1.214), mom6 ^{hl} (0.806), mom12 ^{hl} (0.787), ma50 ^{hl} (0.753).
Volatility	0	tvolf_w ^{lh} (4.437), ivolcapm_d ^{lh} (4.214), tvolf_d ^{lh} (4.164), ivolff_w ^{lh} (4.022), ivolff_d ^{lh} (3.881), ivolcapm_w ^{lh} (3.736), beta ^{lh} (2.639).	0	tvolf_w ^{lh} (1.501), ivolff_w ^{lh} (1.306), tvolf_d ^{lh} (1.247), ivolcapm_w ^{lh} (1.221), ivolcapm_d ^{lh} (1.188), ivolff_d ^{lh} (1.066), beta ^{lh} (0.648).
Growth	2.203	grltnoa ^{lh} (4.935), issue ^{lh} (4.543), issue5 ^{lh} (4.390), agr ^{lh} (3.834), acc ^{lh} (2.596).	0.368	issue ^{lh} (1.055), agr ^{lh} (0.949), issue5 ^{lh} (0.832), grltnoa ^{lh} (0.781), invest_LWZ ^{lh} (0.666), acc ^{lh} (0.516), invest_AG ^{lh} (0.410).
Profitability	2.445	opa ^{hl} (2.863)	0.666	opa ^{hl} (0.869)
Trading	0	illiq ^{hl} (3.876), zerotrade ^{hl} (3.493), std_dvol ^{lh} (3.235), to12 ^{lh} (2.644), turn ^{lh} (2.321), std_turn ^{lh} (2.315), dvol ^{lh} (2.242).	0	zerotrade ^{hl} (0.859), illiq ^{hl} (0.816), to12 ^{lh} (0.684), turn ^{lh} (0.595), std_turn ^{lh} (0.548), std_dvol ^{lh} (0.540), dvol ^{lh} (0.432).
Others	3.378	chceq ^{lh} (4.852), chnco ^{lh} (3.762), invtr ^{lh} (3.603), pchin ^{lh} (3.573), chin ^{lh} (3.459), cashprod ^{lh} (3.425).	0.813	chceq ^{lh} (1.108), bas12 ^{lh} (1.089), maxret ^{lh} (0.942).
All-but-tiny stocks.				
Value	2.570	cfp ^{hl} (4.079)	0.531	cfp ^{hl} (0.889), sp ^{hl} (0.753), bm ^{hl} (0.659), ep ^{hl} (0.614).
Momentum	2.339	wh52 ^{hl} (4.367), ma100 ^{hl} (2.734), mom6 ^{hl} (2.660), ma200 ^{hl} (2.524).	0.617	wh52 ^{hl} (0.834), ma200 ^{hl} (0.684), ma100 ^{hl} (0.663).
Volatility	0	tvolf_w ^{lh} (3.386), beta ^{lh} (3.359), tvolf_d ^{lh} (3.201), ivolcapm_w ^{lh} (3.065), ivolff_w ^{lh} (2.580), ivolff_d ^{lh} (2.286), ivolcapm_d ^{lh} (2.156).	0	tvolf_w ^{lh} (0.960), beta ^{lh} (0.856), tvolf_d ^{lh} (0.790), ivolcapm_w ^{lh} (0.778), ivolff_w ^{lh} (0.652), ivolff_d ^{lh} (0.543), ivolcapm_d ^{lh} (0.508).
Growth	2.338	issue5 ^{lh} (4.440), issue ^{lh} (3.979), grltnoa ^{lh} (3.509), agr ^{lh} (3.336).	0.368	issue ^{lh} (0.953), issue5 ^{lh} (0.844), agr ^{lh} (0.814), invest_LWZ ^{lh} (0.647), grltnoa ^{lh} (0.587), invest_AG ^{lh} (0.392).
Profitability	2.587	–	0.587	–
Trading	2.200	std_dvol ^{lh} (3.040), dvol ^{lh} (2.978), turn ^{lh} (2.394), zerotrade ^{hl} (2.374).	0.002	turn ^{lh} (0.616), zerotrade ^{hl} (0.611), to12 ^{lh} (0.566), std_turn ^{lh} (0.458), std_dvol ^{lh} (0.427), dvol ^{lh} (0.404), illiq ^{hl} (0.279).
Others	3.355	chceq ^{lh} (3.999), chin ^{lh} (3.955), chnco ^{lh} (3.800), pchin ^{lh} (3.518), invtr ^{lh} (3.516).	0.763	chceq ^{lh} (0.945), bas12 ^{lh} (0.929)

Selective inference (3-Factor)

	Studentized		Non-studentized	
	CV	Significant portfolios	CV	Significant portfolios
All stocks.				
Value		#		
Momentum	2.159	ma200^{hl} (5.786), wh52^{hl} (5.576), ma100^{hl} (5.511), mom12_ia^{hl} (4.278), ma50^{hl} (4.215), mom12^{hl} (4.141), mom6^{hl} (3.406).	0.563	ma200^{hl} (1.529), ma100^{hl} (1.415), wh52^{hl} (1.389), mom12^{hl} (1.089), ma50^{hl} (1.071), mom12_ia^{hl} (0.904), mom6^{hl} (0.854).
Volatility	2.046	ivolcapm.d^{lh} (4.936), tvolf.w^{lh} (4.849), ivolff.d^{lh} (4.732), ivolff.w^{lh} (4.564), tvolf.d^{lh} (4.319), ivolcapm.w^{lh} (4.202).	0.471	tvolf.w^{lh} (1.335), ivolff.w^{lh} (1.221), tvolf.d^{lh} (1.158), ivolcapm.d^{lh} (1.152), ivolcapm.w^{lh} (1.128), ivolff.d^{lh} (1.026).
Growth	2.383	issue^{lh} (4.314), grltnoa^{lh} (4.073), issue5^{lh} (4.016), agr^{lh} (2.967), acc^{lh} (2.618).	0.488	issue^{lh} (0.818), issue5^{lh} (0.810), grltnoa^{lh} (0.595), agr^{lh} (0.524), acc^{lh} (0.514).
Profitability	2.464	opa^{hl} (3.100)	0.623	opa^{hl} (0.925)
Trading	2.523	illiq^{hl} (4.523), std.dvol^{lh} (2.701).	0.481	illiq^{hl} (0.623).
Others	3.380	chceq^{lh} (3.903), bas12^{lh} (3.723).	0.702	bas12^{lh} (1.035), mom1^{hl} (0.846), chceq^{lh} (0.779), maxret^{lh} (0.739).
All-but-tiny stocks.				
Value	2.77	-	0.588	-
Momentum	2.186	wh52^{hl} (4.811), ma200^{hl} (3.861), mom12_ia^{hl} (3.852), ma100^{hl} (3.509), ma50^{hl} (3.277), mom12^{hl} (3.270), mom6^{hl} (2.597).	0.490	ma200^{hl} (0.988), wh52^{hl} (0.915), ma100^{hl} (0.903), ma50^{hl} (0.764), mom12^{hl} (0.725), mom12_ia^{hl} (0.702), mom6^{hl} (0.620).
Volatility	2.488	tvolf.w^{lh} (3.085), ivolcapm.w^{lh} (2.745), tvolf.d^{lh} (2.696), beta^{lh} (2.686), ivolff.w^{lh} (2.218).	0.414	tvolf.w^{lh} (0.672), ivolcapm.w^{lh} (0.565), beta^{lh} (0.560), tvolf.d^{lh} (0.539), ivolff.w^{lh} (0.450).
Growth	2.488	issue^{lh} (4.128), issue5^{lh} (3.888), grltnoa^{lh} (2.936).	0.502	issue5^{lh} (0.750), issue^{lh} (0.731).
Profitability	2.388	opa^{hl} (2.607), gmr^{hl} (2.571).	0.559	opa^{hl} (0.616)
Trading		#		
Others	3.396	-	0.655	mom1^{hl} (0.699)

Selective inference (4-Factor)

	Studentized		Non-studentized	
	CV	Significant portfolios	CV	Significant portfolios
All stocks.				
Value	#			
Momentum	2.544	–	0.615	ma100^{hl} (0.741), ma200^{hl} (0.682), wh52^{hl} (0.641).
Volatility	1.995	tvolf_w^{lh} (4.214), ivolf_w^{lh} (3.894), ivolcapm_d^{lh} (3.832), ivolcapm_w^{lh} (3.827), tvolf_d^{lh} (3.467), ivolf_d^{lh} (3.402).	0.495	tvolf_w^{lh} (1.162), ivolf_w^{lh} (1.061), ivolcapm_w^{lh} (1.013), ivolcapm_d^{lh} (0.976), tvolf_d^{lh} (0.962), ivolf_d^{lh} (0.834).
Growth	2.492	issue^{lh} (4.032), issue5^{lh} (3.327), grltnoa^{lh} (3.108).	0.503	issue^{lh} (0.754), issue5^{lh} (0.707), grltnoa^{lh} (0.511).
Profitability	2.437	opa^{hl} (2.607)	0.603	opa^{hl} (0.782)
Trading	2.540	illiq^{hl} (3.863)	0.455	illiq^{hl} (0.539)
Others	3.399	–	0.718	–
All-but-tiny stocks.				
Value	2.751	–	0.551	–
Momentum	#			
Volatility	2.446	–	0.516	–
Growth	2.612	issue^{lh} (3.824), issue5^{lh} (3.091).	0.493	issue^{lh} (0.662), issue5^{lh} (0.599).
Profitability	2.490	gmr^{hl} (2.611)	0.565	–
Trading	#			
Others	3.463	–	0.674	–

Selective inference (5-Factor)

	Studentized		Non-studentized	
	CV	Significant portfolios	CV	Significant portfolios
All stocks.				
Value	2.709	cfp_ia^{hl} (2.878)	0.624	–
Momentum	2.617	ma50^{hl} (5.017), ma200^{hl} (4.646), ma100^{hl} (4.415), mom12ia^{hl} (3.690), wh52^{hl} (3.545), mom12^{hl} (3.391), mom6^{hl} (2.742).	0.567	ma200^{hl} (1.420), ma100^{hl} (1.314), ma50^{hl} (1.259), wh52^{hl} (0.942), mom12^{hl} (0.912), mom12ia^{hl} (0.864), mom6^{hl} (0.805).
Volatility	2.294	tvolf_w^{lh} (2.780), ivolcapm_d^{lh} (2.694), ivolff_w^{lh} (2.350).	0.518	tvolf_w^{lh} (0.617), ivolff_w^{lh} (0.551), ivolcapm_d^{lh} (0.534).
Growth	2.605	invest_LWZ^{hl} (3.140)	0.449	invest_LWZ^{hl} (0.612) acc^{lh} (0.509)
Profitability	2.616	–	0.600	–
Trading	2.610	illiq^{hl} (4.359)	0.484	illiq^{hl} (4.359)
Others	3.394	mom1^{hl} (4.505), noa^{lh} (3.961), chfn^{hl} (3.740), ma20^{hl} (3.526).	0.674	mom1^{hl} (1.140), ma20^{hl} (0.840), chpm^{hl} (0.761), noa^{lh} (0.757).
All-but-tiny stocks.				
Value	2.769	–	0.533	–
Momentum	2.393	ma50^{hl} (4.700), mom12_ia^{hl} (4.017), ma200^{hl} (3.697), ma100^{hl} (3.195), mom12^{hl} (3.074), wh52^{hl} (2.931).	0.606	ma50^{hl} (1.091), ma200^{hl} (1.038), ma100^{hl} (0.990), mom12_ia^{hl} (0.785), mom12^{hl} (0.688).
Volatility		#		
Growth	2.870	invest_LWZ^{hl} (3.488)	0.432	invest_LWZ^{hl} (0.685)
Profitability	2.860	–	0.494	–
Trading		#		
Others	3.493	noa^{lh} (4.916), mom1^{hl} (4.458), quick^{hl} (4.316), salecash^{lh} (4.219), ma20^{hl} (3.863), pchsale^{hl} (3.817), debteq^{lh} (3.708).	0.646	mom1^{hl} (1.063), ma20^{hl} (0.995), salecash^{lh} (0.714), quick^{hl} (0.695), noa^{lh} (0.692), chpm^{hl} (0.669), tangible^{hl} (0.656).

Selective inference (Q-Factor)

	Studentized		Non-studentized	
	CV	Significant portfolios	CV	Significant portfolios
All stocks.				
Value	2.710	cfp_ia^{hl} (3.144)	0.794	–
Momentum	2.472	ma200^{hl} (2.531)	0.774	ma200^{hl} (0.844).
Volatility	2.552	–	0.749	–
Growth	2.653	–	0.573	invest_LWZ^{hl} (0.692).
Profitability	2.633	–	0.759	–
Trading	2.549	illiq^{hl} (3.437)	0.647	–
Others	3.407	–	0.904	–
All-but-tiny stocks.				
Value	2.843	bm_ia^{hl} (2.907)	0.709	–
Momentum	2.730	–	0.895	–
Volatility	#			
Growth	2.771	–	0.524	invest_LWZ^{hl} (0.825)
Profitability	2.709	–	0.652	–
Trading	#			
Others	3.514	–	0.874	–

4 Pre- versus post-1993 period comparison

Pre- versus post-1993 comparison (all stocks)

		CAPM	3-Factor	4-Factor	5-Factor
Studentized test.					
Pre-1993	FWER(1)	15 (3.345)	18 (3.390)	9 (3.359)	7 (3.514)
	FWER(2)	24 (2.976)	22 (2.975)	14 (3.021)	12 (3.094)
	FWER(3)	31 (2.756)	29 (2.747)	17 (2.783)	13 (2.857)
	$t > 1.96$	53	49	37	29
Post-1993	FWER(1)	2 (3.382)	8 (3.431)	1 (3.443)	1 (3.503)
	FWER(2)	4 (3.033)	13 (3.032)	3 (3.050)	4 (3.111)
	FWER(3)	10 (2.800)	16 (2.814)	9 (2.834)	7 (2.888)
	$t > 1.96$	31	41	27	13
Non-studentized test.					
Pre-1993	FWER(1)	11 (1.043)	15 (0.896)	10 (0.919)	1 (1.009)
	FWER(2)	20 (0.892)	24 (0.721)	12 (0.761)	4 (0.865)
	FWER(3)	21 (0.819)	27 (0.659)	16 (0.688)	7 (0.777)
Post-1993	FWER(1)	3 (1.447)	9 (1.112)	3 (1.133)	3 (1.152)
	FWER(2)	4 (1.317)	14 (0.950)	4 (0.992)	4 (0.995)
	FWER(3)	6 (1.233)	15 (0.874)	6 (0.903)	6 (0.911)

Pre- versus post-1993 comparison (all-but-tiny stocks)

		CAPM	3-Factor	4-Factor	5-Factor
Studentized test.					
Pre-1993	FWER(1)	7 (3.380)	6 (3.432)	0 (3.493)	1 (3.473)
	FWER(2)	18 (2.995)	16 (3.035)	4 (3.050)	1 (3.093)
	FWER(3)	23 (2.774)	19 (2.806)	6 (2.869)	3 (2.900)
	$t > 1.96$	50	37	24	17
Post-1993	FWER(1)	0 (3.389)	2 (3.464)	1 (3.445)	0 (3.561)
	FWER(2)	2 (3.047)	4 (3.083)	2 (3.043)	1 (3.166)
	FWER(3)	4 (2.872)	9 (2.898)	4 (2.856)	1 (2.942)
	$t > 1.96$	22	26	16	18
Non-studentized test.					
Pre-1993	FWER(1)	3 (0.900)	5 (0.843)	0 (0.857)	0 (0.975)
	FWER(2)	10 (0.768)	8 (0.688)	2 (0.700)	0 (0.817)
	FWER(3)	15 (0.712)	14 (0.621)	4 (0.632)	0 (0.725)
Post-1993	FWER(1)	0 (1.398)	3 (1.022)	1 (1.004)	2 (1.003)
	FWER(2)	1 (1.287)	5 (0.915)	2 (0.892)	5 (0.857)
	FWER(3)	2 (1.215)	7 (0.842)	3 (0.831)	5 (0.780)